

# **Evidence for scattering of curvature radiation in radio pulsar profiles**

Jaroslaw Dyks

Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences

*MNRAS* 522, 1480–1490 (2023)

Reporter: 曹顺顺  
(Shunshun Cao)

2024.12

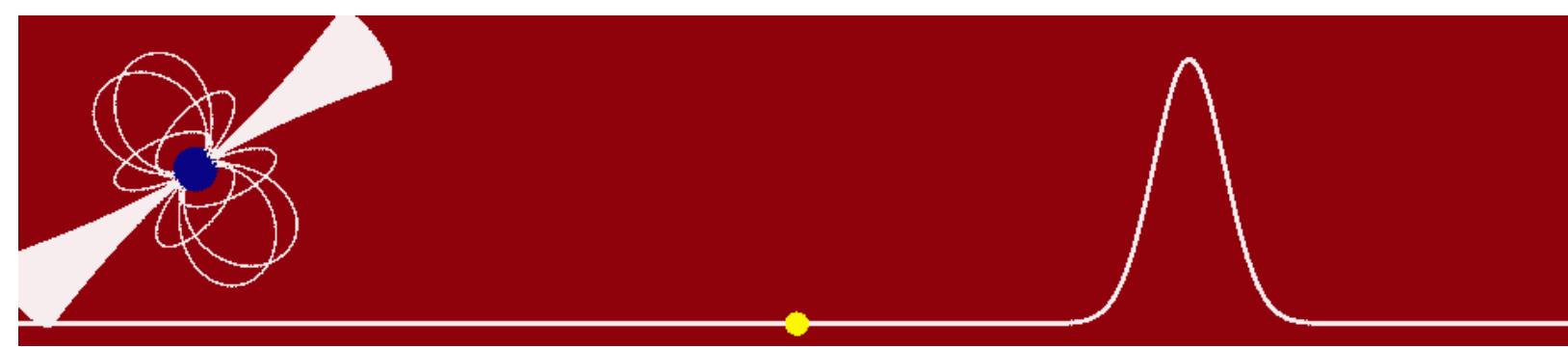
23 pages in total



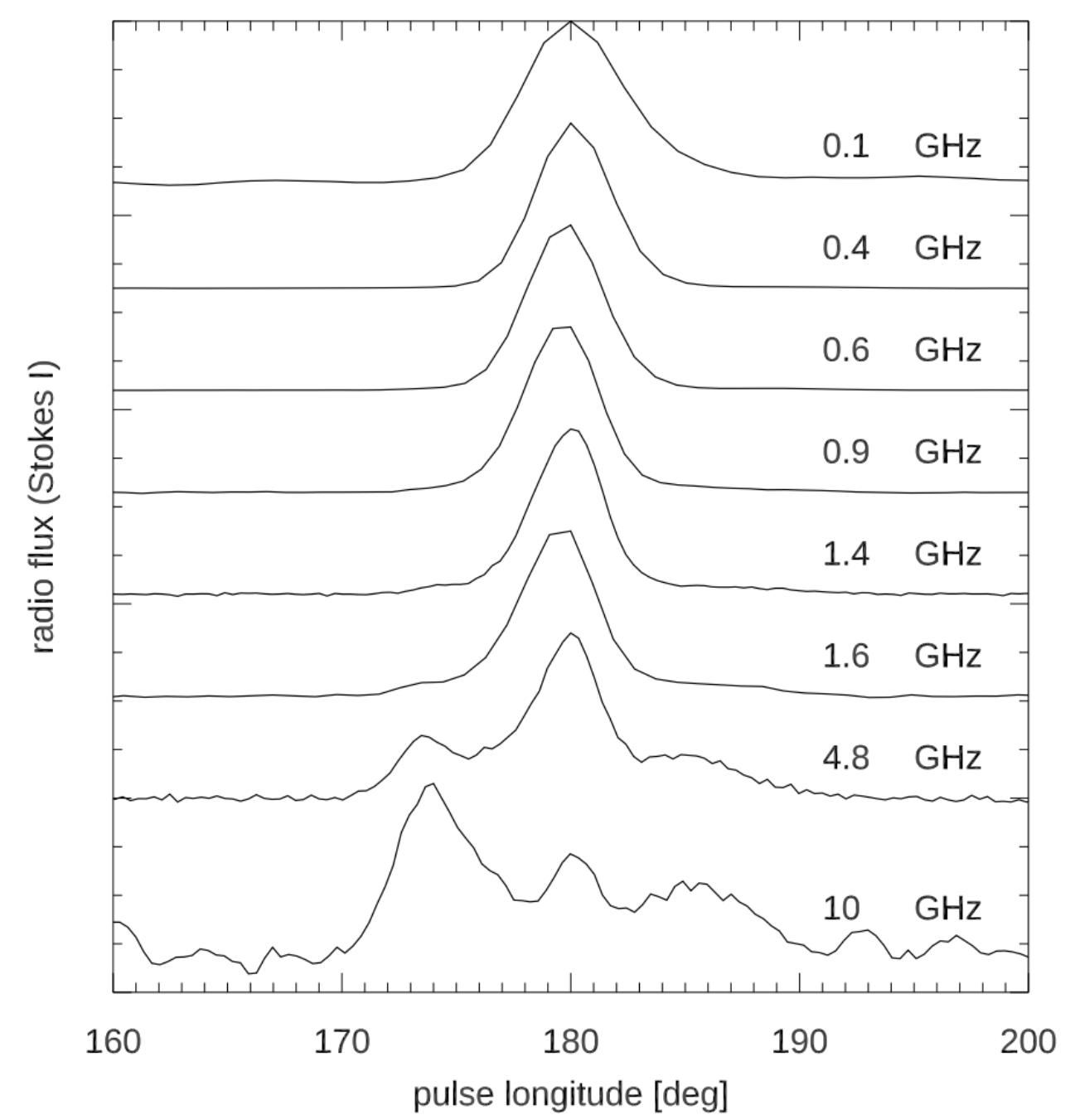
# I. Introduction

Pulsar signal: hundreds of single pulses  
→ integrated profile (usually steady).

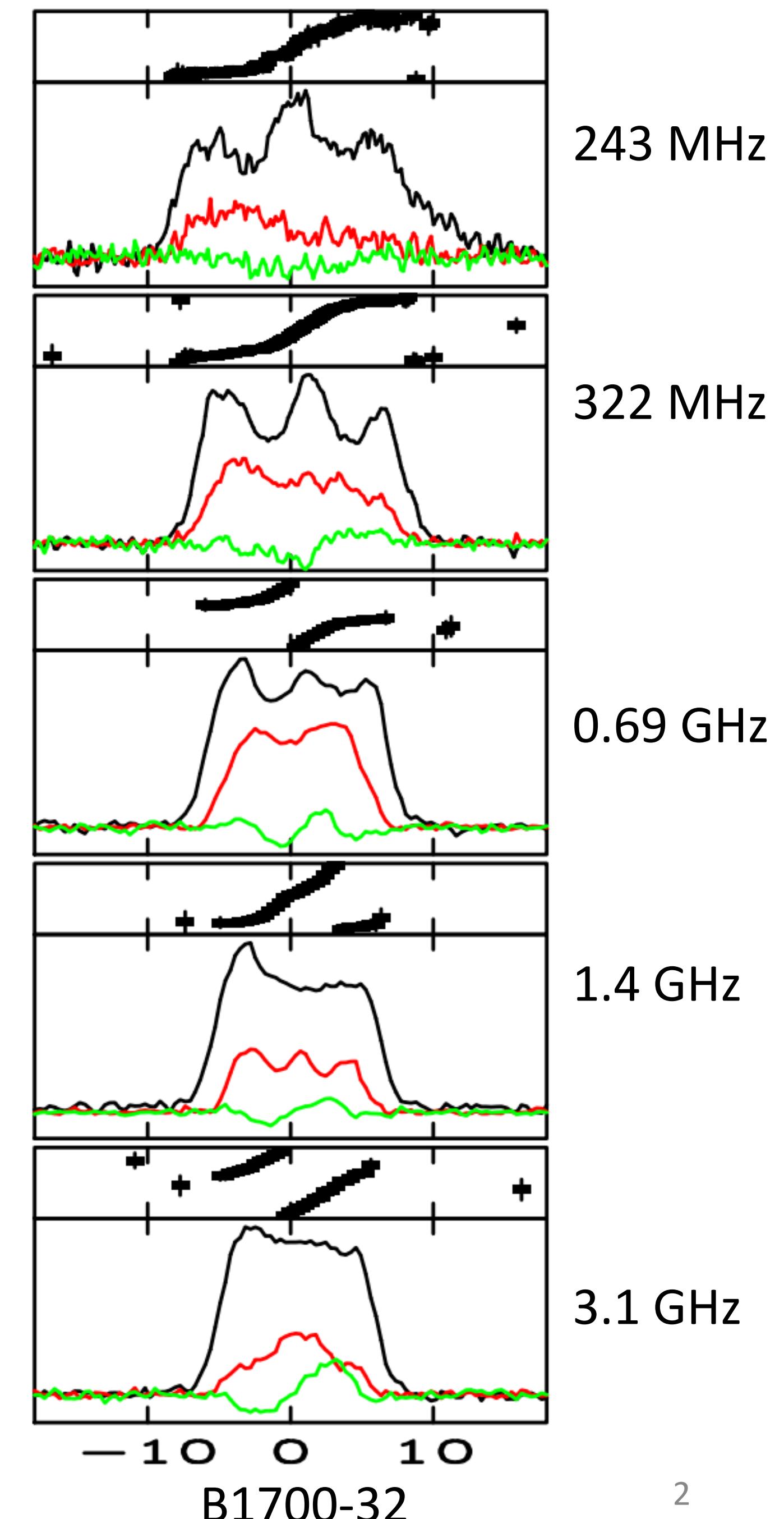
Integrated profiles are rich in morphology,  
and could evolve with frequency.



[psr.pku.edu.cn](http://psr.pku.edu.cn)

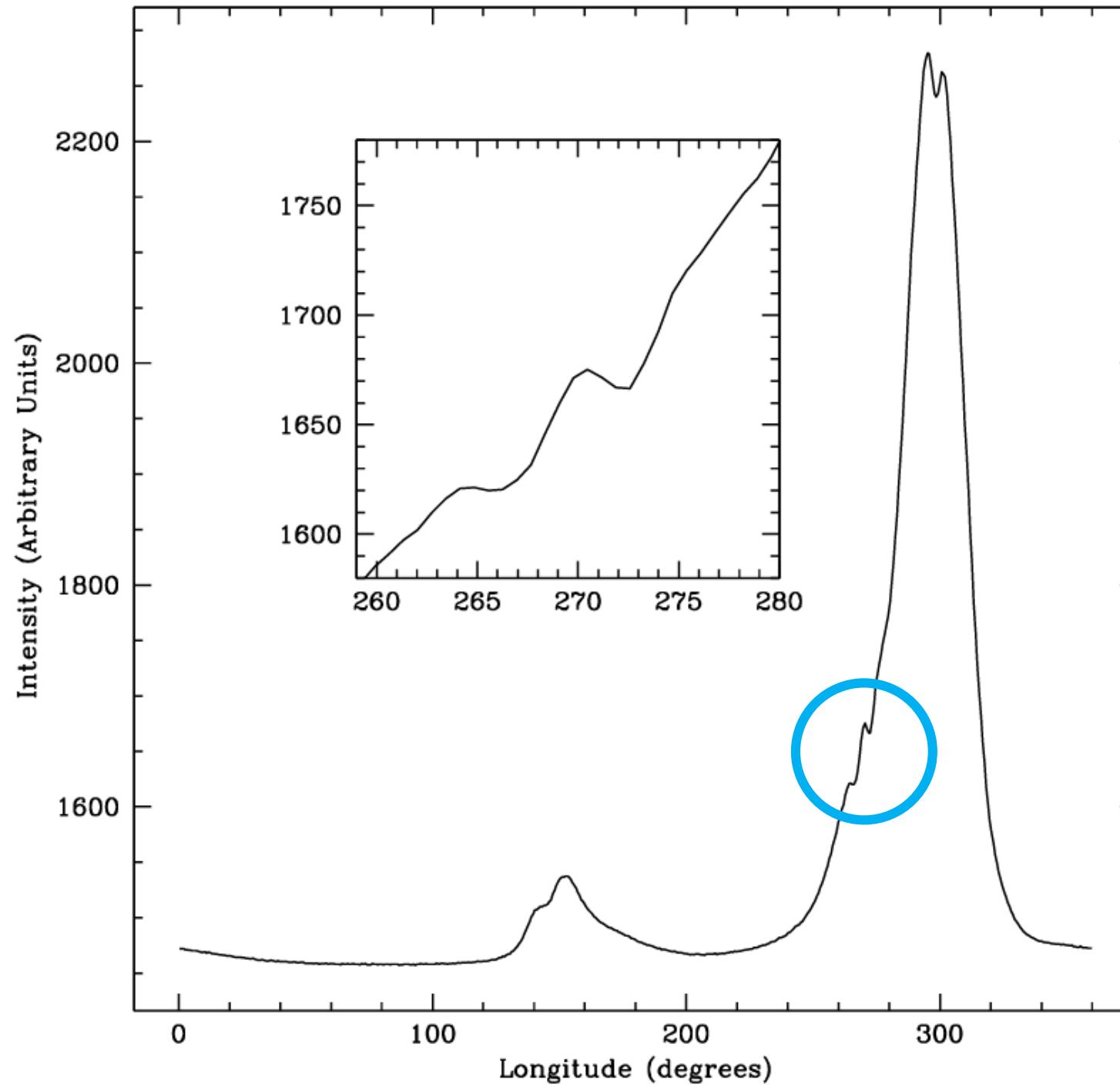


B1642-03



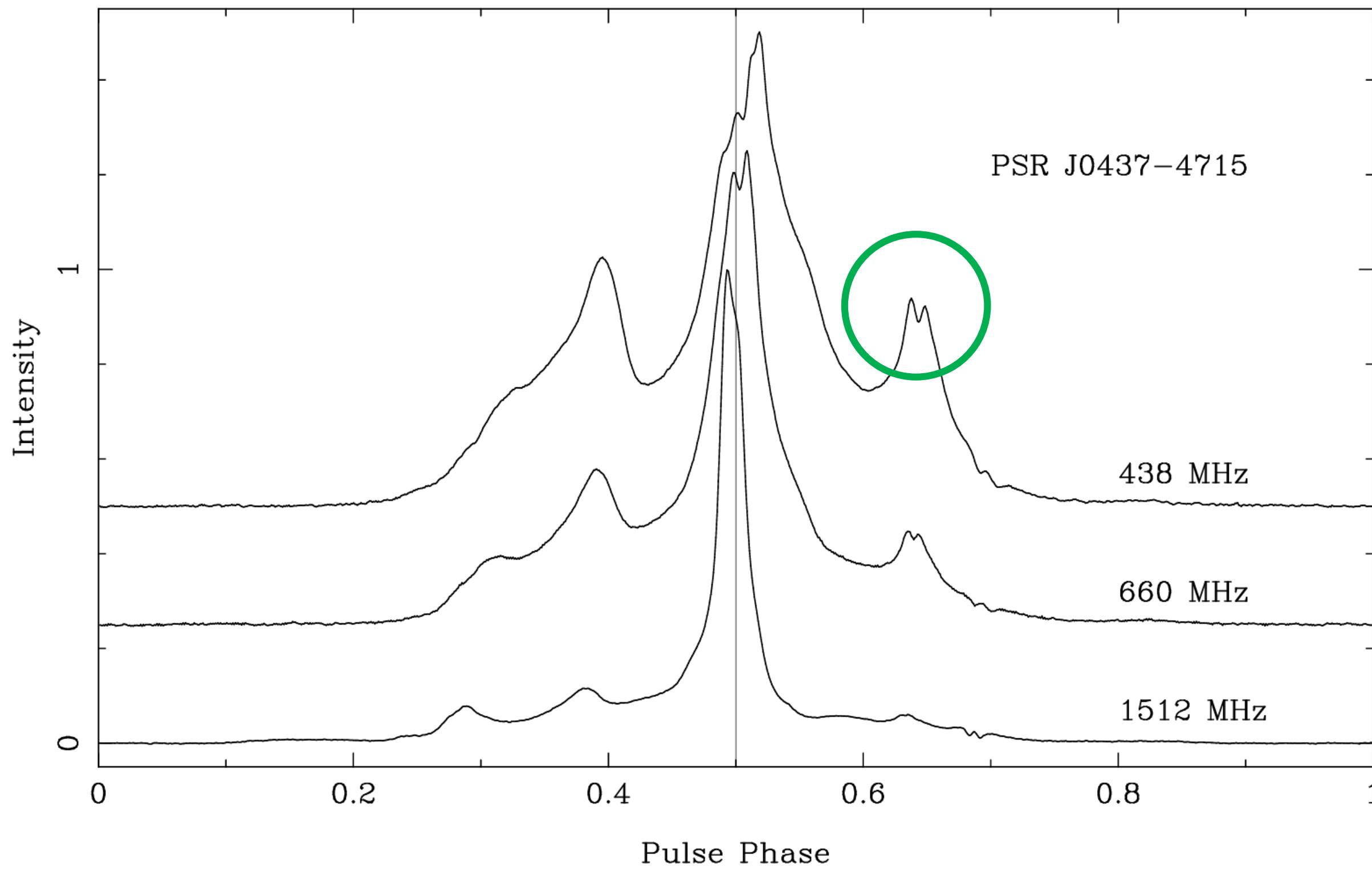
# A special kind of profile property: bifurcated components (BCs)

Double notches (DNs):

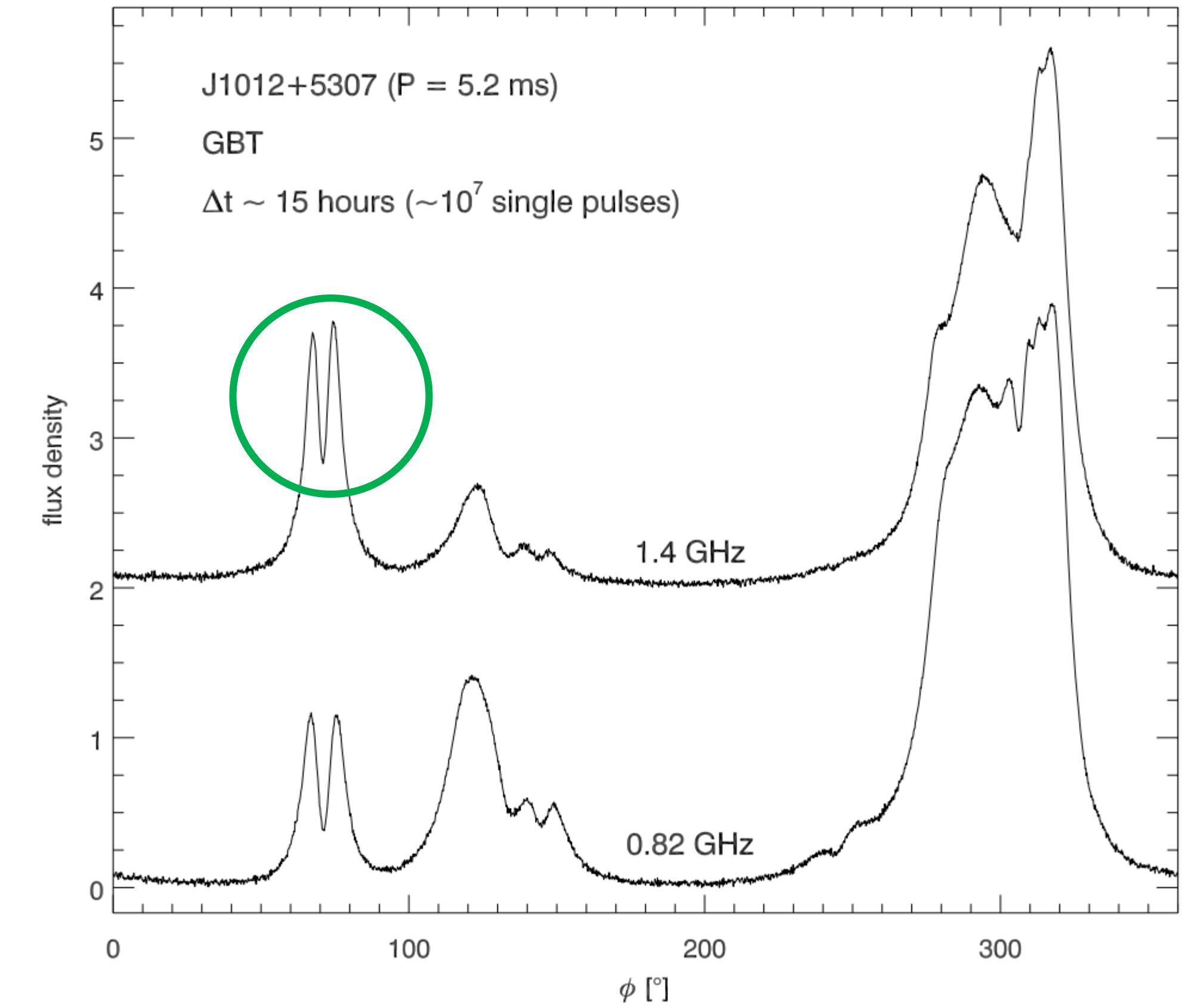


# A special kind of profile property: bifurcated components (BCs)

Bifurcated peaks:



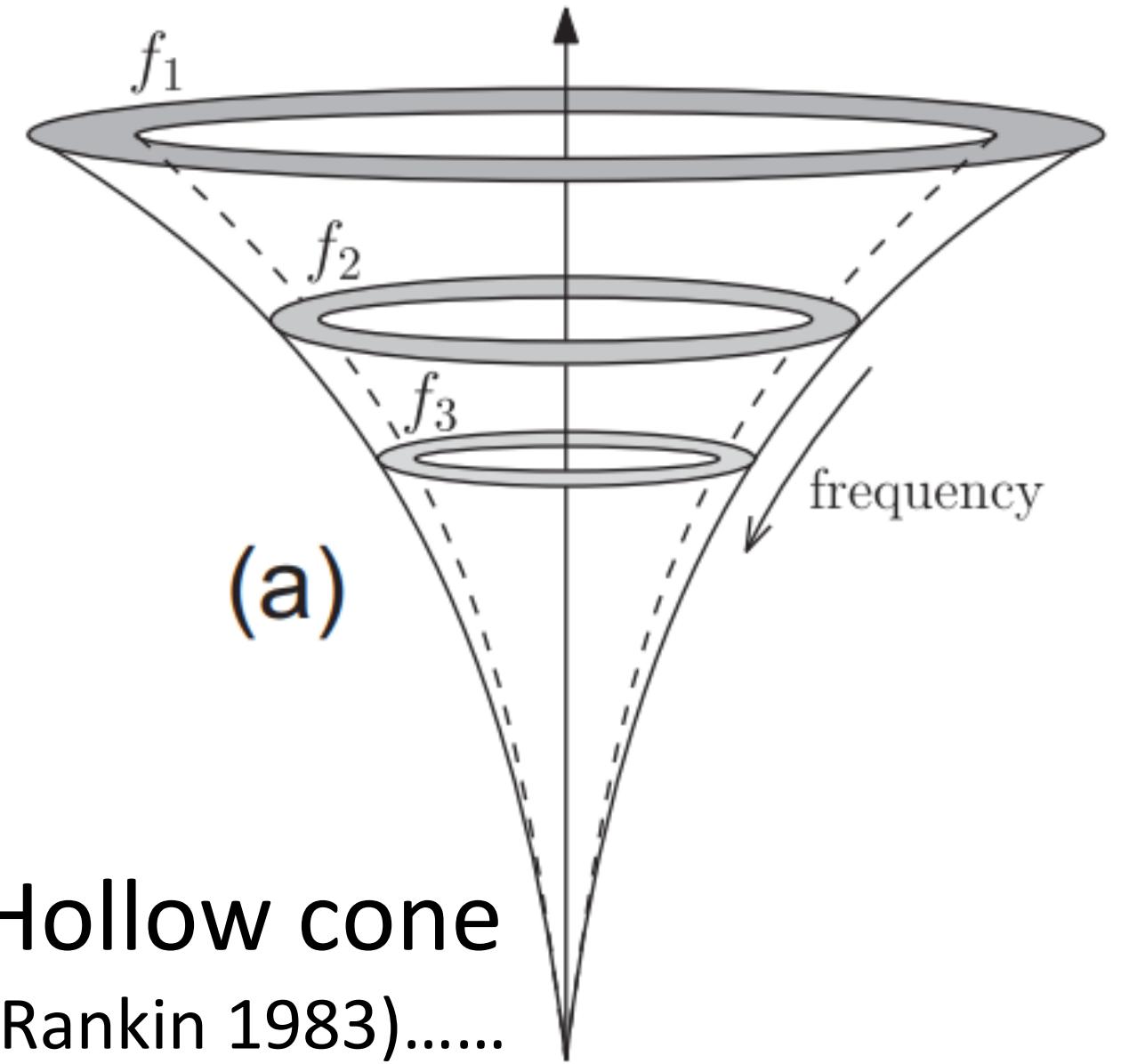
J0437-4715  
Navarro et al. 1997 *ApJ*



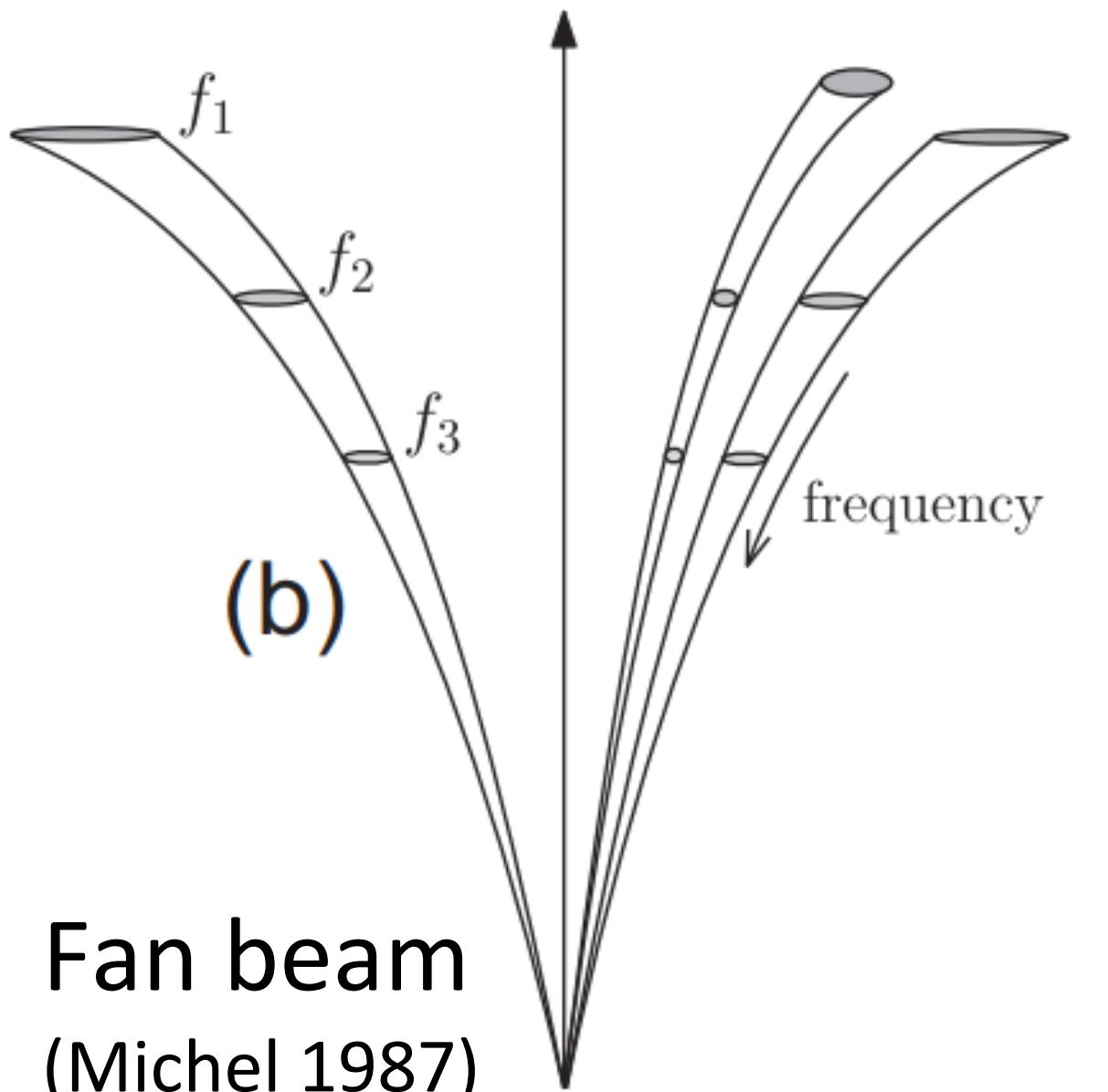
J1012+5307  
Dyks, Rudak & Demorest 2010 *MNRAS*

Explanations to phenomena:

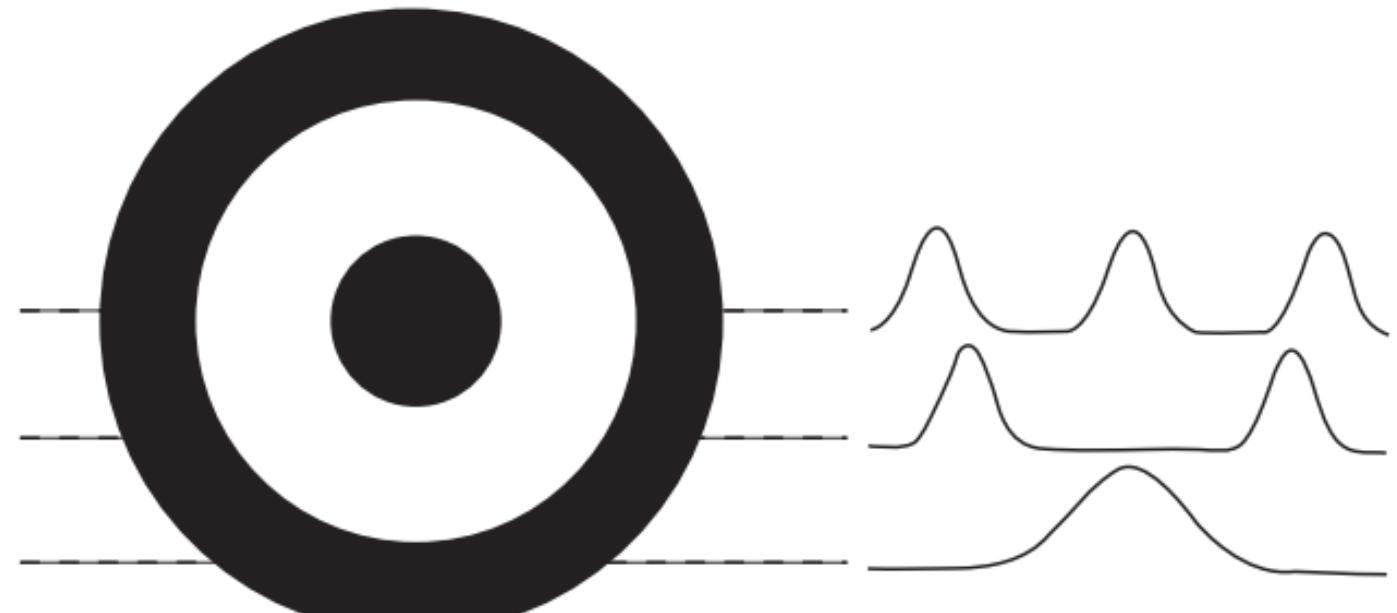
“Conal components” & “Core component”: What’s the physical origin?



Hollow cone  
(Rankin 1983).....

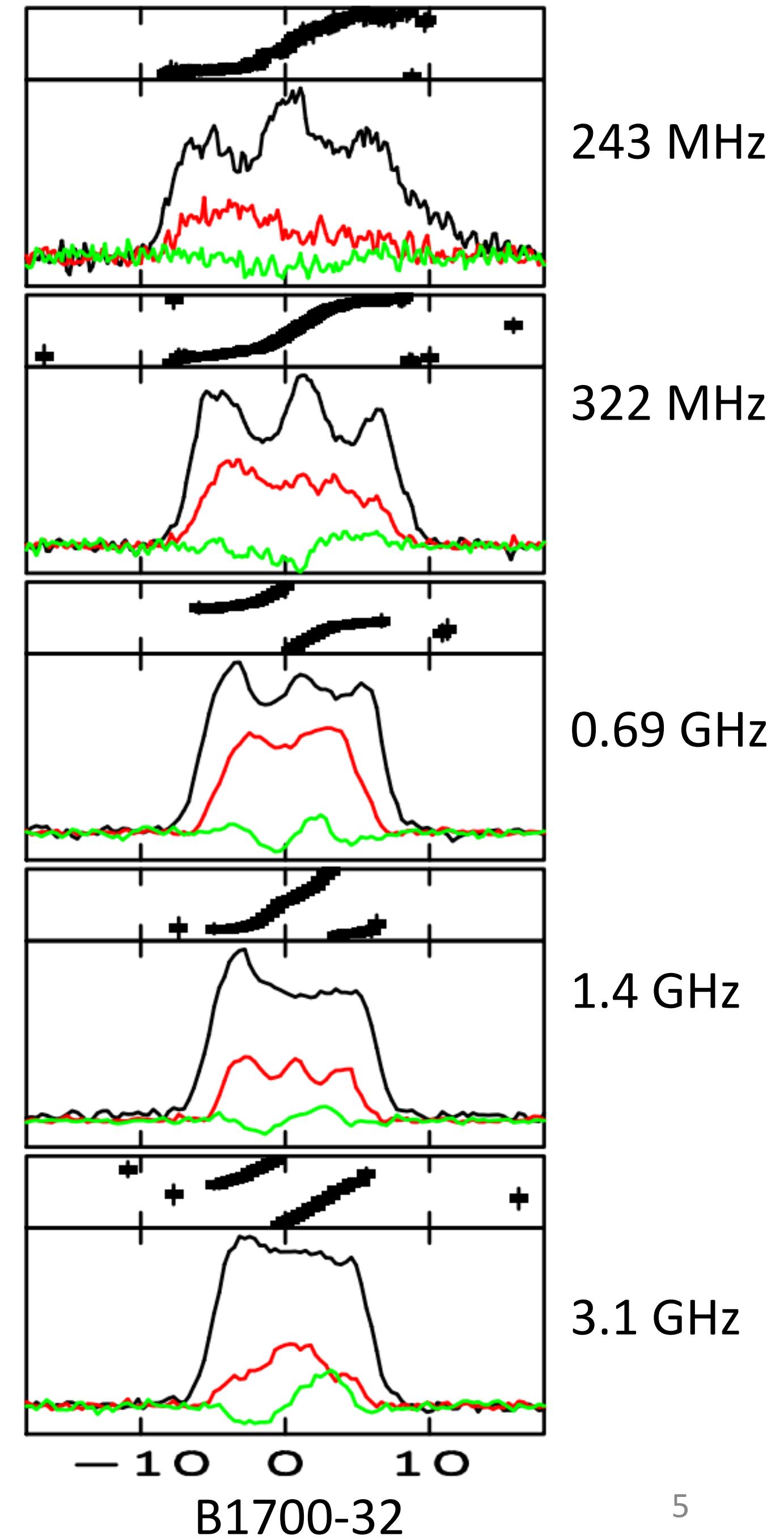


Fan beam  
(Michel 1987)  
(Dyks, Rudak & Demorest 2010)  
(Wang et al. 2014).....



From *Pulsar Astronomy*

Emission of different frequencies  
may come from different heights  
→ Radius-to-frequency mapping  
(RFM)

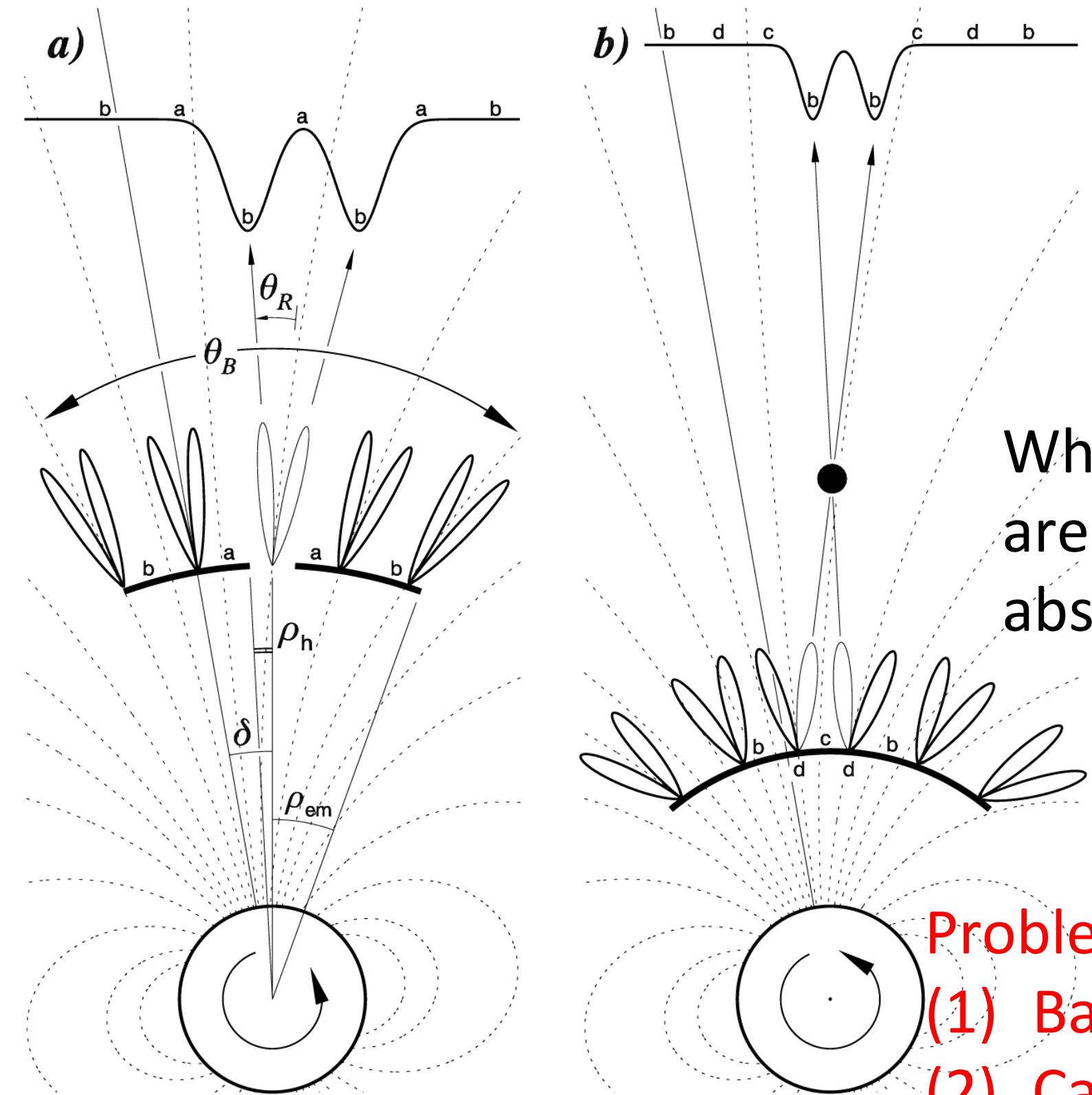


# Explanations to phenomena:

What's behind bifurcated components?

Dyks, Rudak & Rankin 2007 A&A: direction of acceleration?

Emission from parallel-accelerated particles is naturally bifurcated.



When part of emission particles are lost or part of emission is absorbed, double notches appear.

Problem (Dyks, Rudak, Demorest 2010):  
 (1) Bad fitting of J1012+5037 (1.4 GHz).  
 (2) Cannot produce too deep notch.

Dyks, Rudak & Rankin 2007 A&A

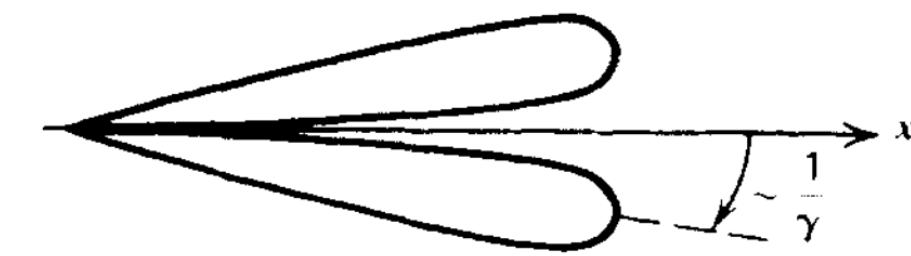


Figure 4.11b Angular distribution of radiation emitted by a particle with parallel acceleration and velocity.

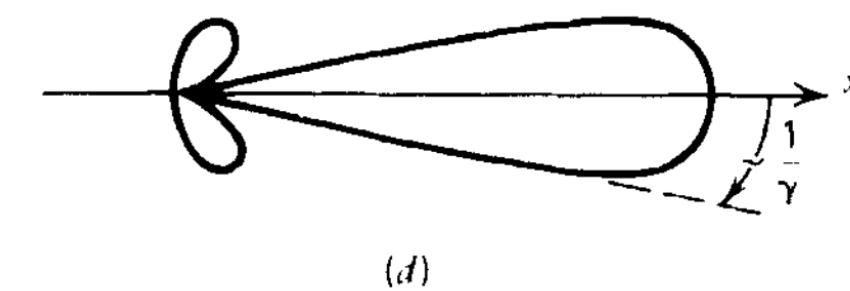
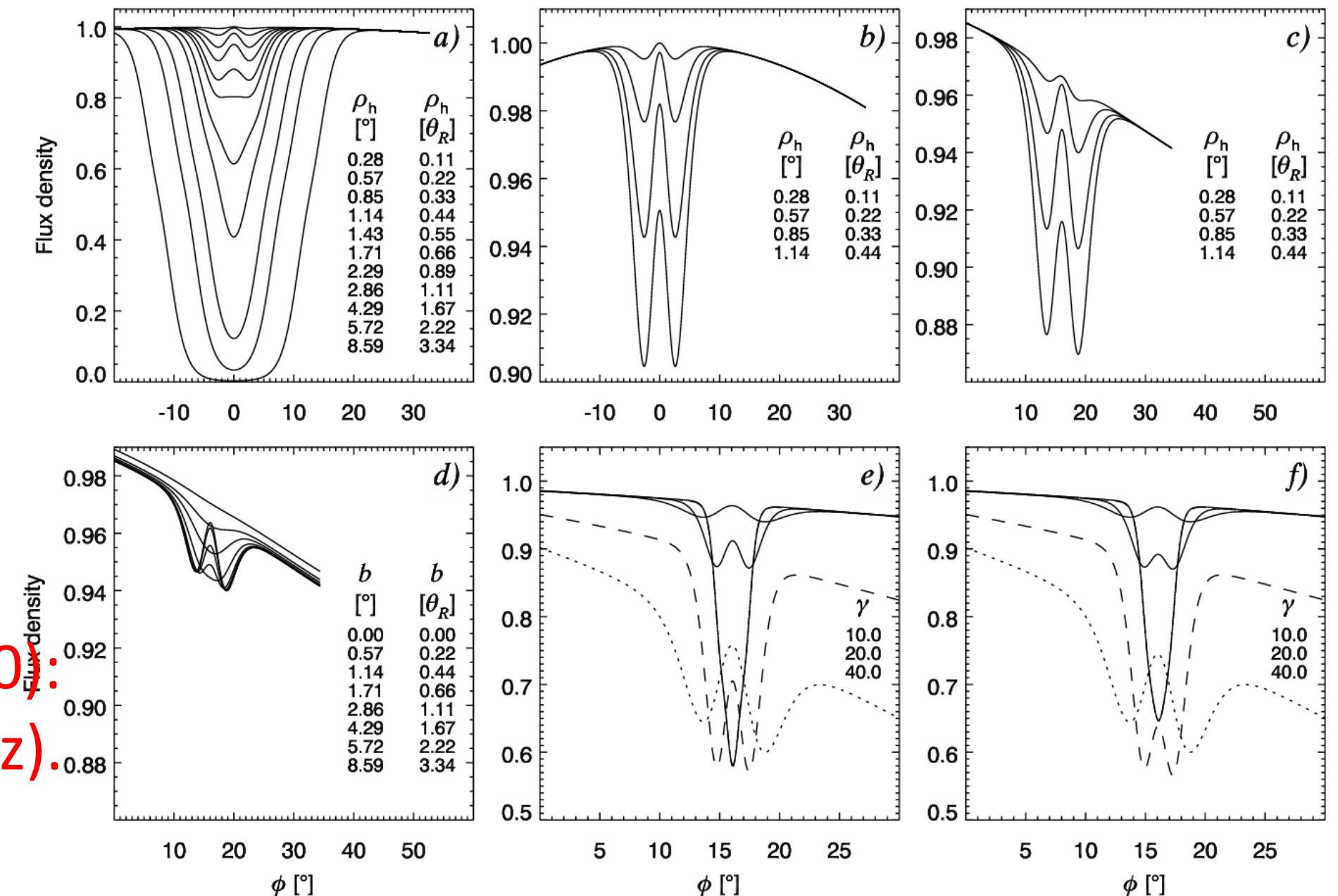


Figure 4.11d Angular distribution of radiation emitted by a particle with perpendicular acceleration and velocity.

From Rybicki & Lightman  
*Radiative Processes in Astrophysics*



Dyks, Rudak & Rankin 2007

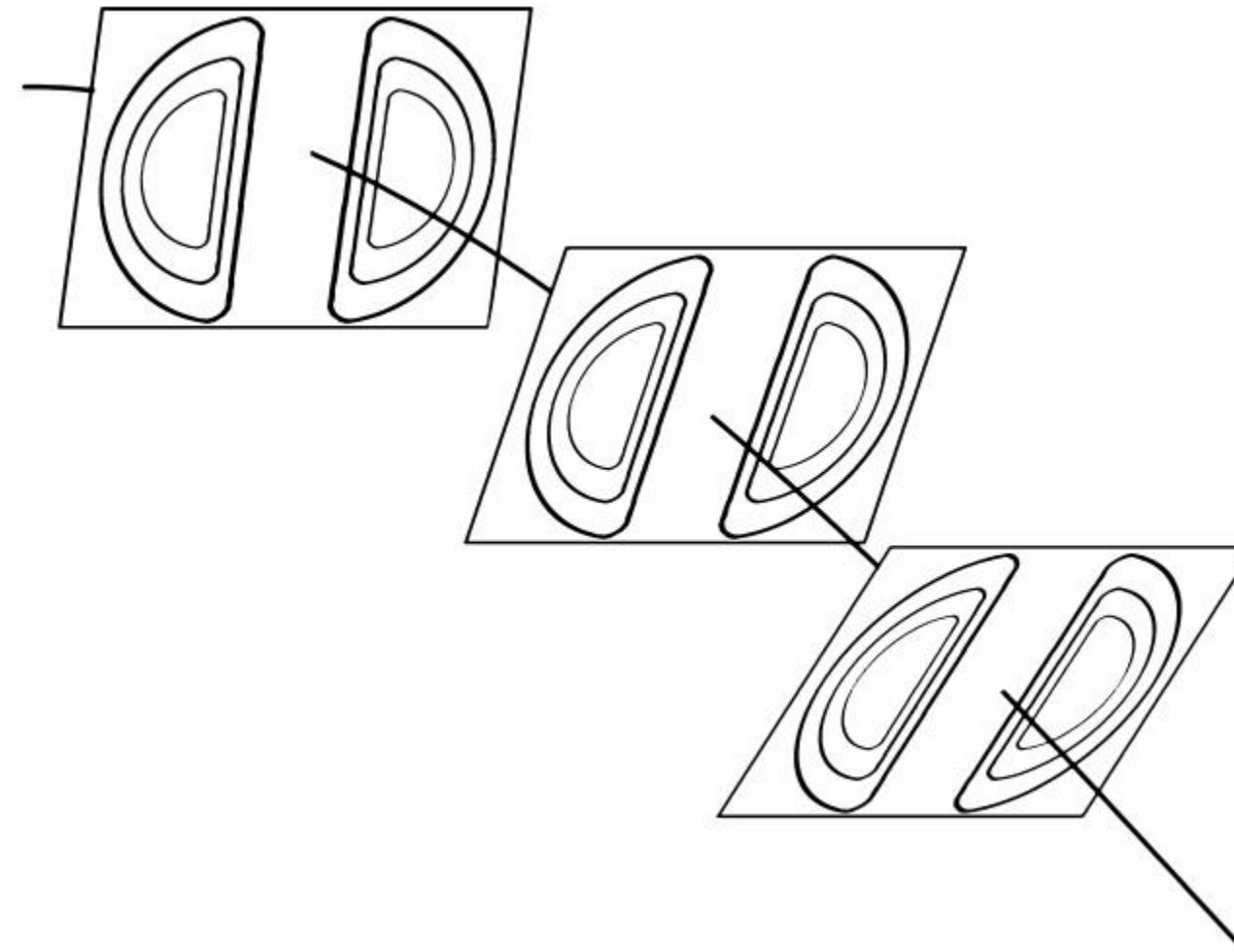
Explanations to phenomena:

What's behind bifurcated components?

Dyks, Rudak & Demorest 2010 MNRAS: consider partial absorption of curvature radiation cone?

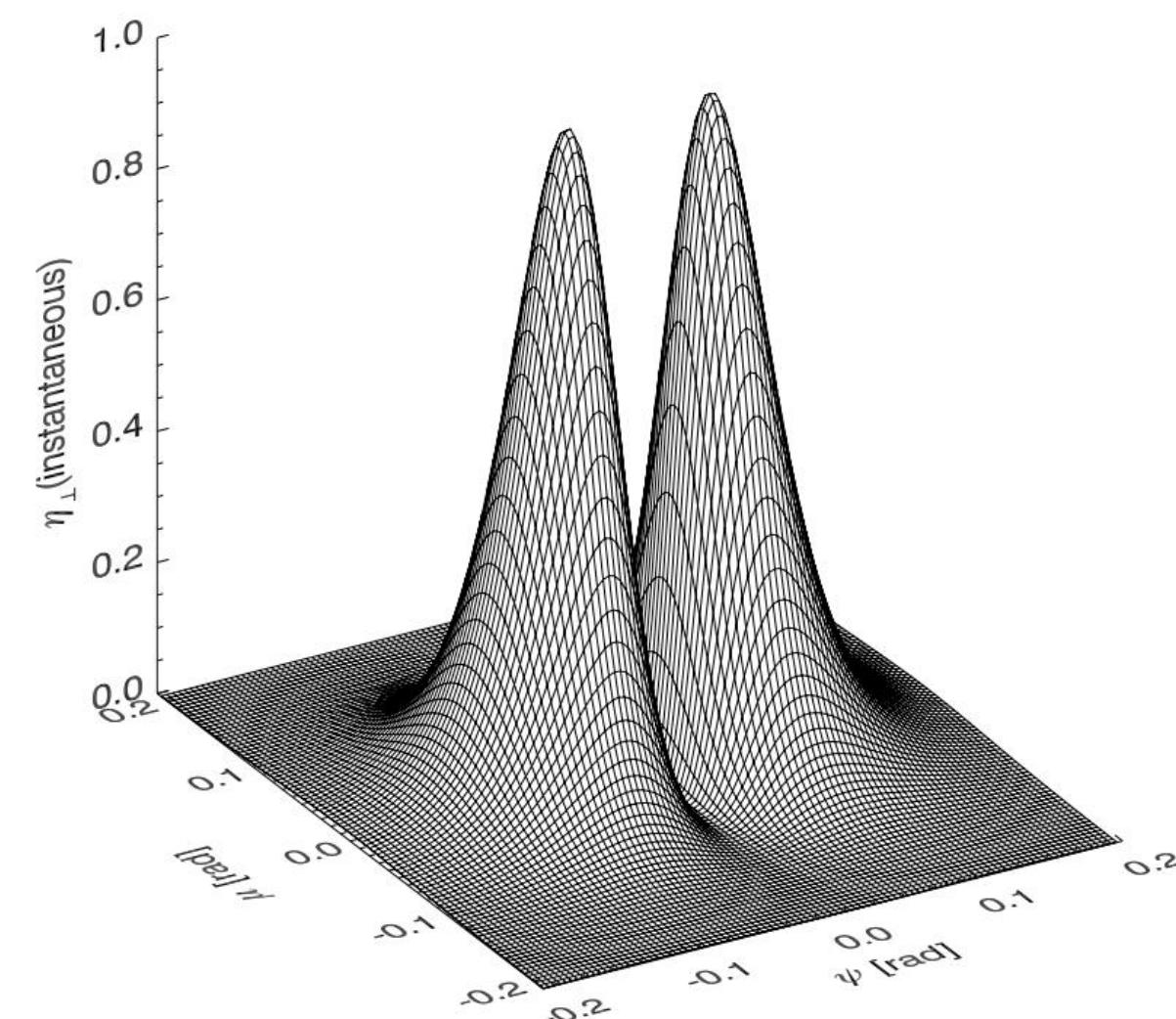
Emission polarized in electron's trajectory plane is more easily absorbed.

→ radiation becomes bifurcated.



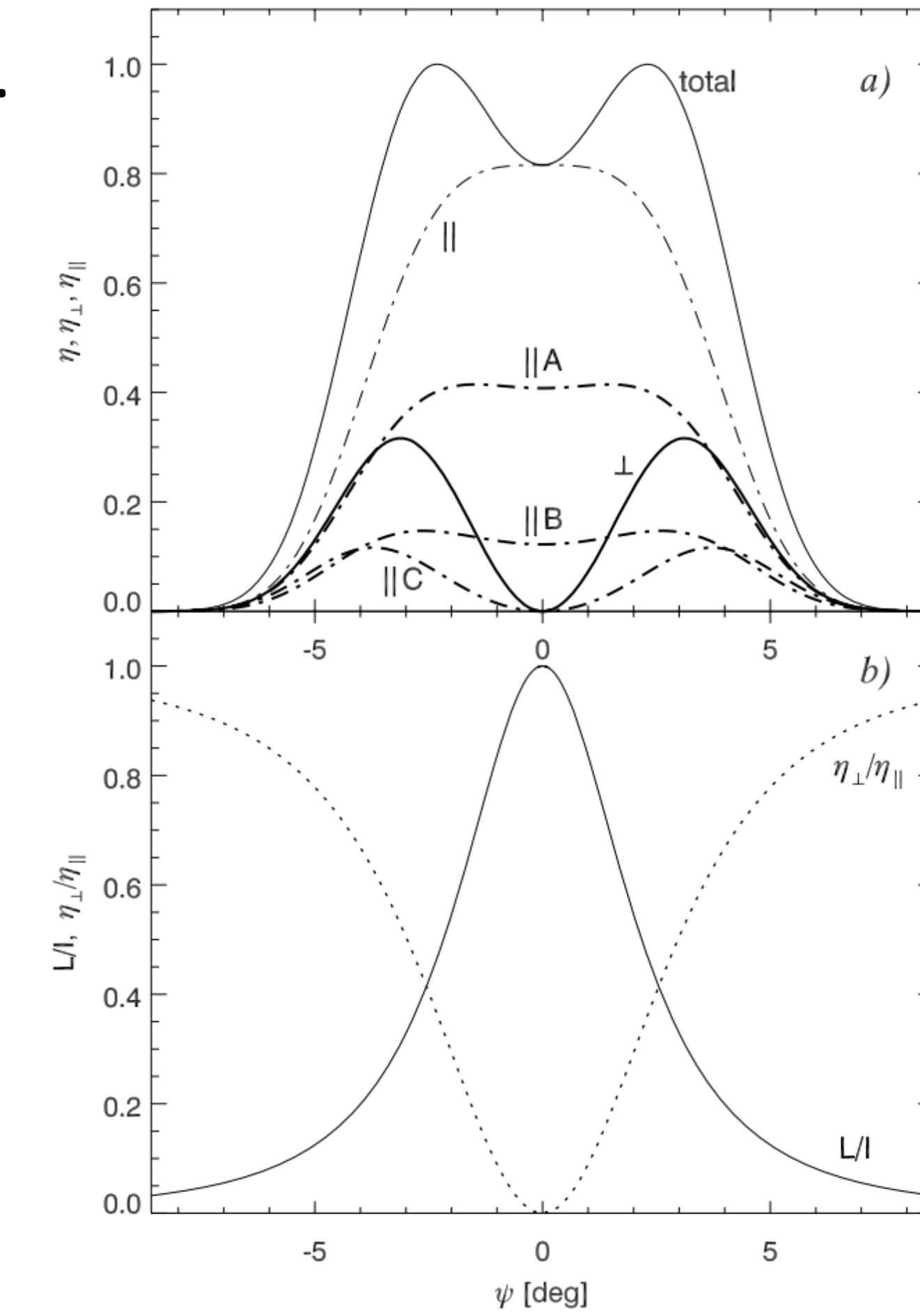
Dyks, Rudak & Demorest 2010

Problem (Dyks 2023):  
 (1) Too narrow profile



$$\eta_{\text{crv}} = \eta_{\parallel} + \eta_{\perp}$$

$$= \frac{q^2 \omega^2}{3\pi^2 c} \left(\frac{\rho}{c}\right)^2 [\xi^2 K_{2/3}^2(y) + \xi K_{1/3}^2(y) \sin^2 \psi],$$



Dyks, Rudak & Demorest 2010

Dyks 2023: consider profiles being modified by inverse Compton scattering (ICS).

ICS: high energy electrons give energy to photons.

When  $\gamma h\nu \ll m_e c^2$  is satisfied (always true for pulsar radio waves) in ICS,  $\nu_1 = \gamma^2 \nu_0$ .

ICS changes the radiation cone morphology, and spectral properties.

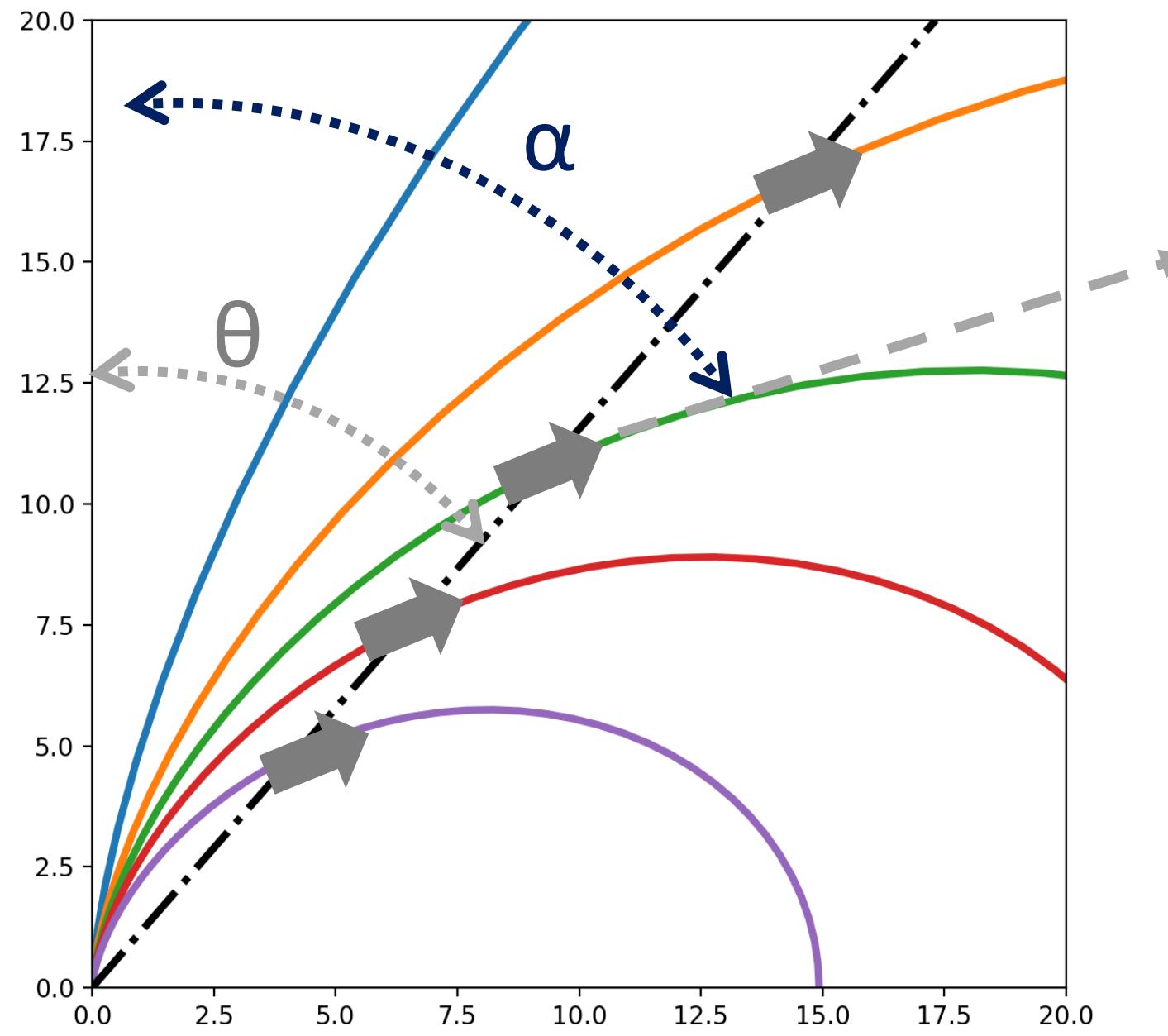
## II. Basic Model for Conal Structure

A photon goes through several following stages in pulsar magnetic field:

- (i) Emitted at some point  $r_{\text{em}}$ ;
- (ii) Propagate through a mean free path  $\eta_{\text{sc}}$ ;
- (iii) Scattered by electrons moving along local B field.

Assume scattered photons propagate in the direction of scattering electron.

↔ in the direction of local B field.

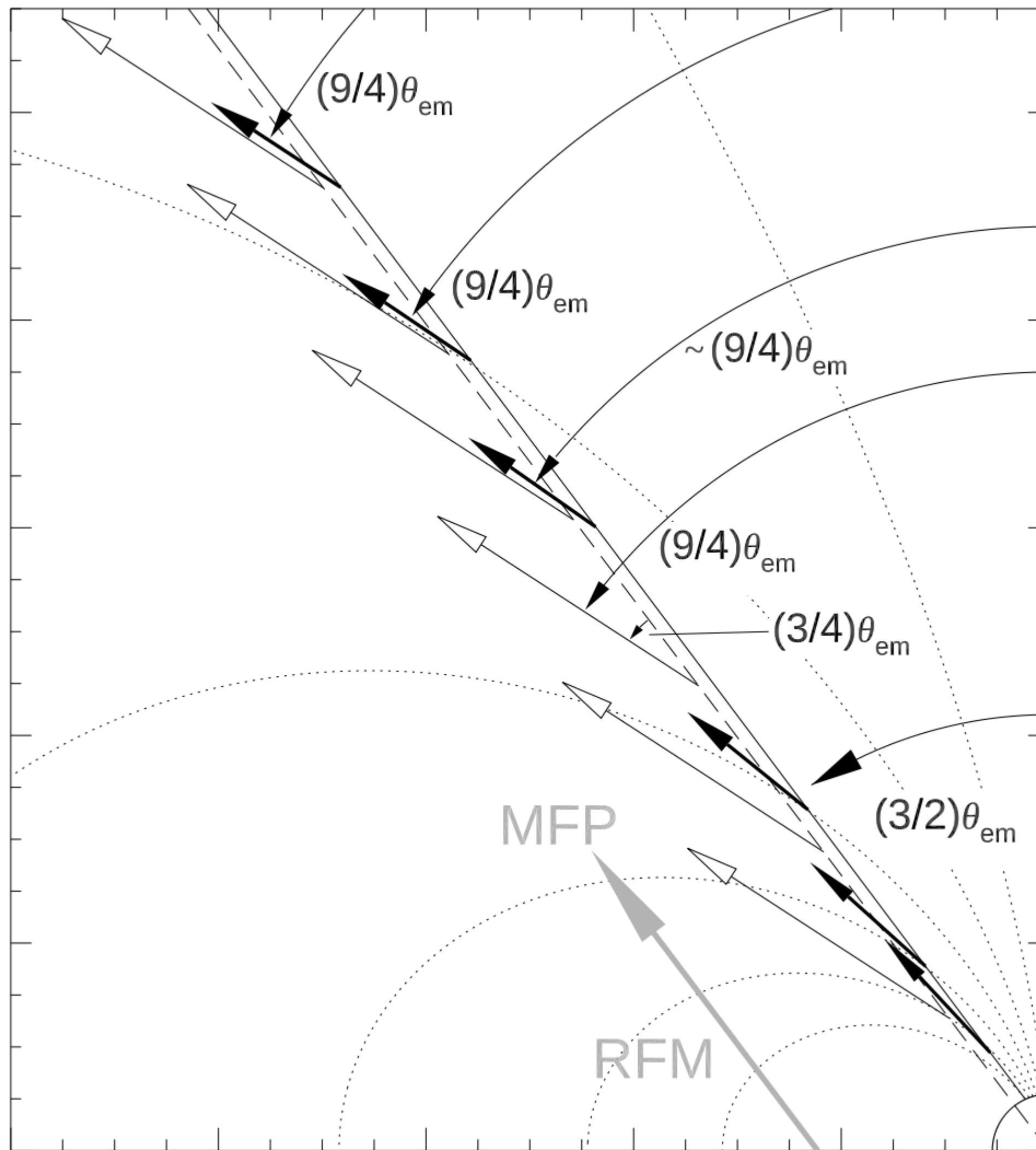


Important property of dipolar field:  
Tangential direction  $\alpha$  only depends on polar angle  $\theta$ .

$$\tan \alpha = \frac{3 \sin \theta \cos \theta}{2 \cos^2 \theta - \sin^2 \theta}$$

When  $\theta \ll 1$  and  $\alpha \ll 1$ :  $\alpha = 3/2 \theta$ .

Apply to formation of conal emission:



Dashed line:

Initial emitting direction (goes through pulsar centroid).

Black solid line:

Initial emitting direction (from emitting point).

White-tip arrows:

B-field directions for points on the dashed line.

Black-tip arrows:

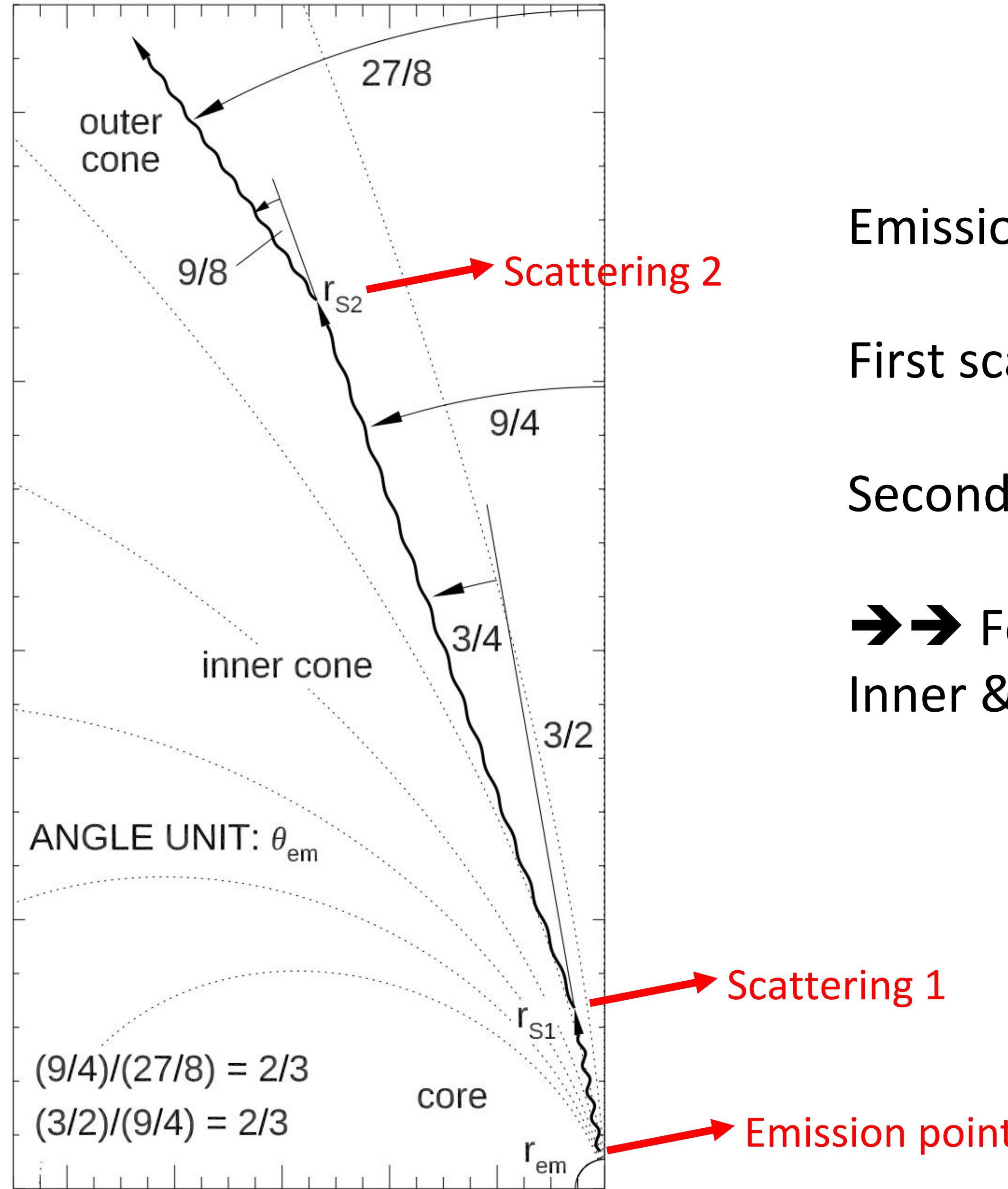
B-field directions for points on the black solid line.

(i.e. ray propagating direction after scattered at this point)

When mean free path of photon is large enough ( $\eta_{sc} \gg r_{em}$ ),  $\alpha = (3/2) * (3/2) \theta = 9/4 \theta$ .

Emission point

If there's second order scattering:



Emission:  $\alpha = 3/2 \theta$

First scattering:  $\alpha = (3/2) * (3/2) \theta = 9/4 \theta$

Second scattering:  $\alpha = (3/2) * (3/2) * (3/2) \theta = 27/8 \theta$

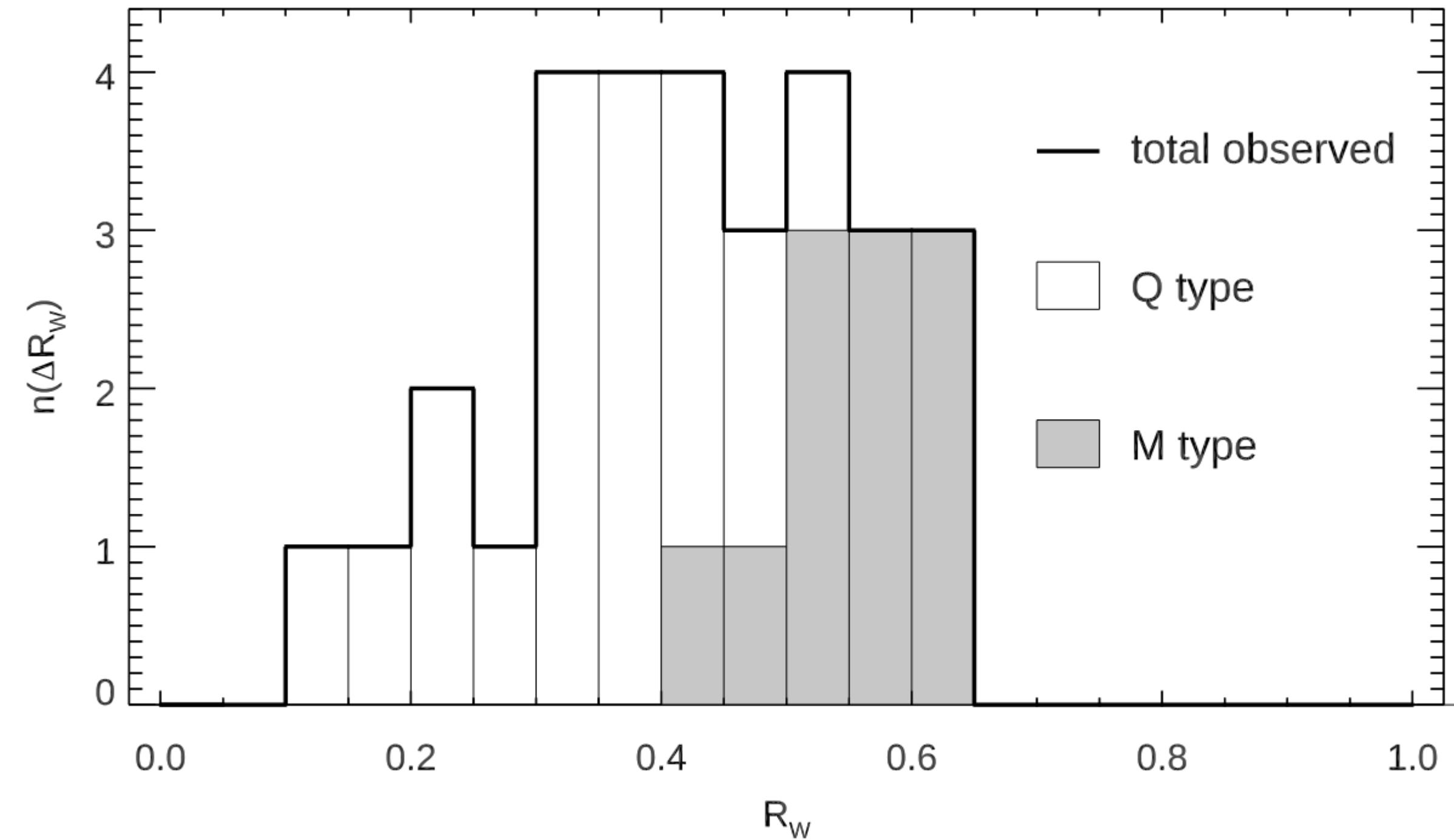
→→ Form inner & outer cones.

Inner & Outer cones' width ratio:

$$R_{io} = \frac{3}{2} \theta_{em} \left( \frac{9}{4} \theta_{em} \right)^{-1} = \frac{2}{3}$$

Comparison with data:

$$R_{\text{io}} = \frac{3}{2} \theta_{\text{em}} \left( \frac{9}{4} \theta_{\text{em}} \right)^{-1} = \frac{2}{3}$$



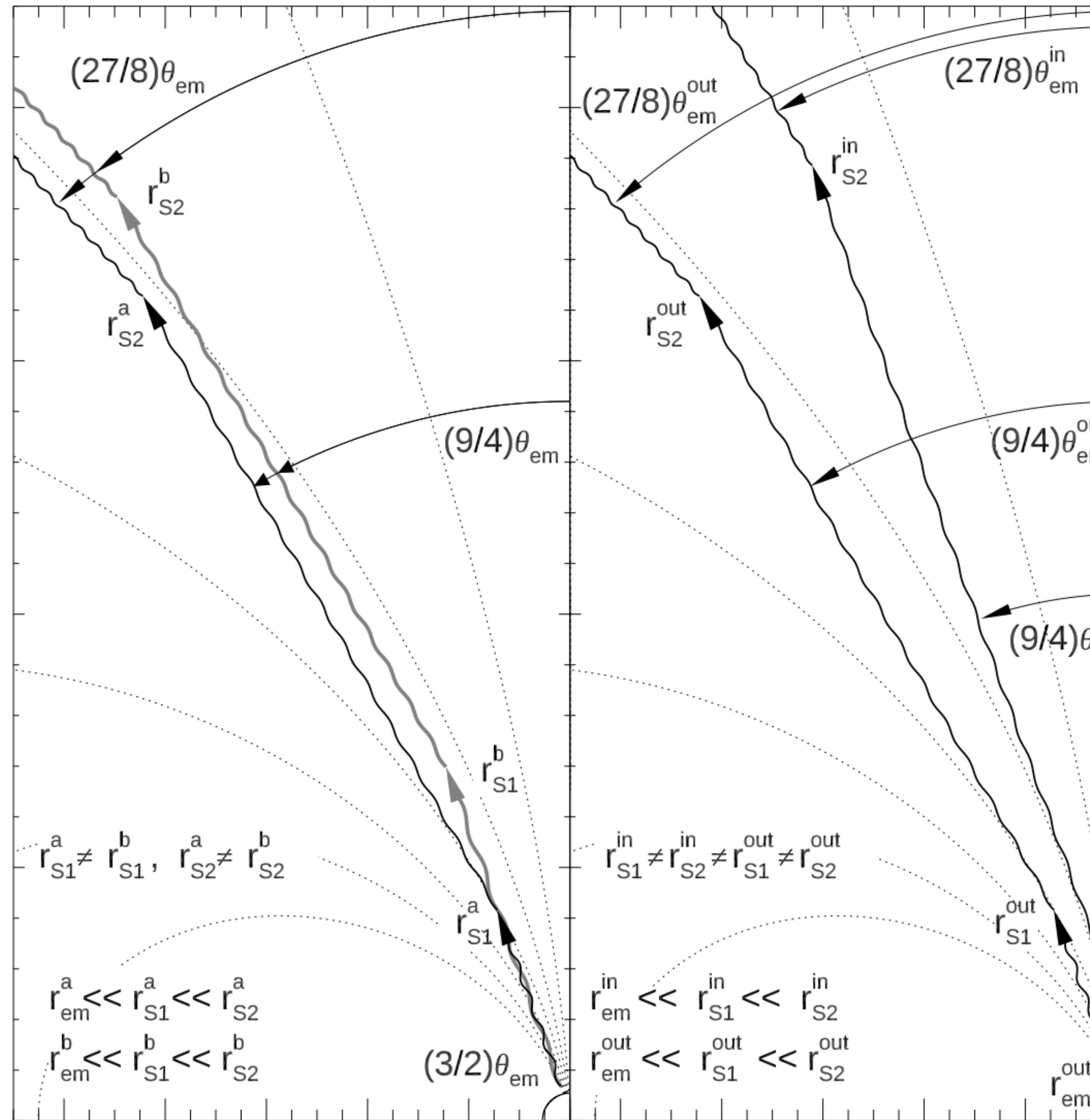
$R$  smaller than  $2/3$   
→ Beam suppression?

Statistics from Dyks & Pierbattista 2015

Q type: 4-components profile

M type: 5-components profile

## Two kinds of ray scattering with long enough mean free path:



Left: two rays emitted at same polar angle;  
 Right: two rays emitted at different polar angle.

→ Forms double cones or core-cone.

Dipolar magnetic field configuration confirms scattering angles to be independent of scattering radii.

→ Non-dipolar: could still be valid for any l-pole star-centered field.

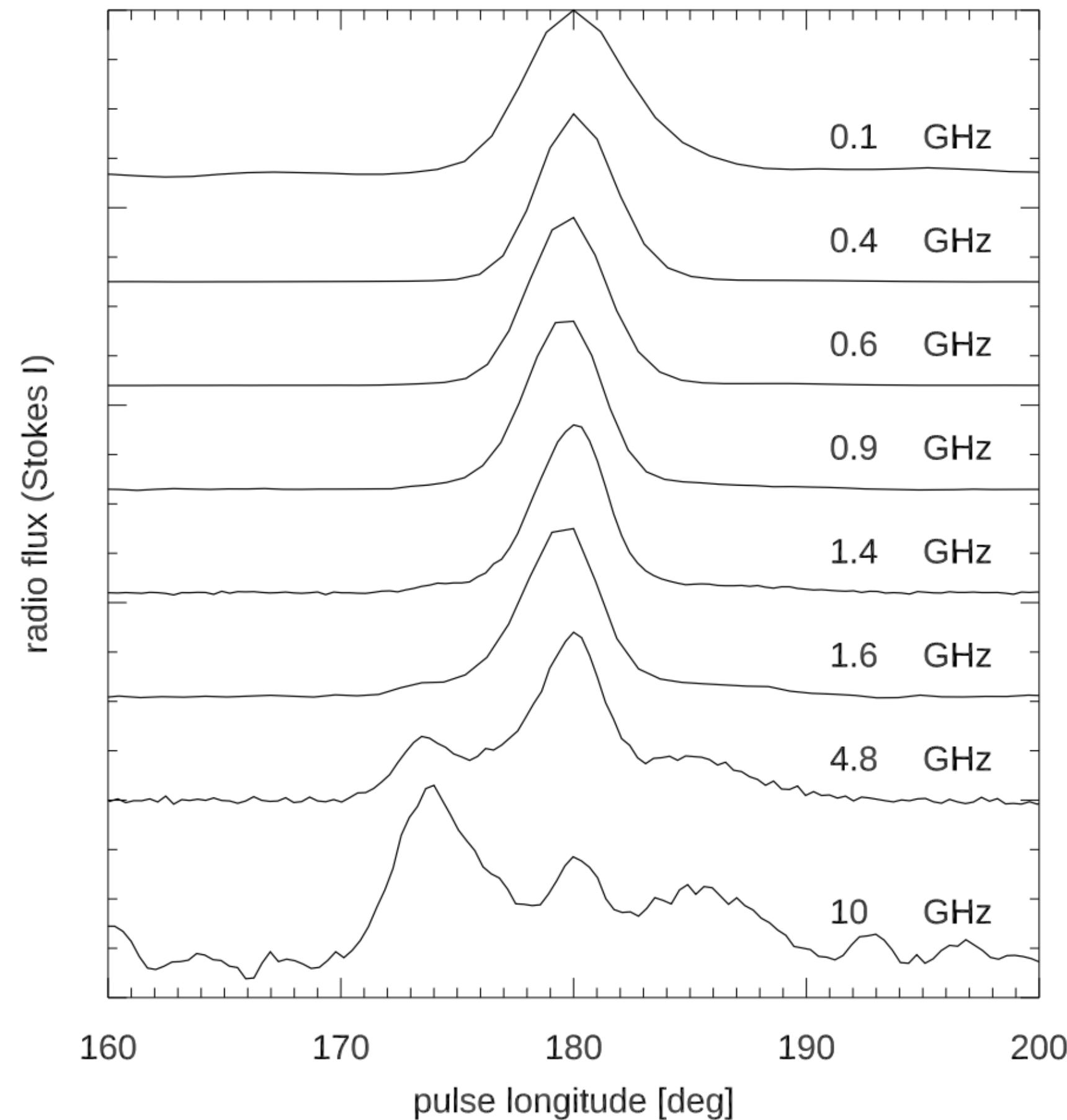
$$B_r = B_{lj} \left( \frac{R_*}{r} \right)^{2+l} P_l(\cos \theta_B) \approx B_{lj} \left( \frac{R_*}{r} \right)^{2+l},$$

$$B_\theta = -\frac{B_{lj}}{l+1} \left( \frac{R_*}{r} \right)^{2+l} dP_l(\cos \theta_B)/d\theta_B \approx B_{lj} \frac{l}{2} \left( \frac{R_*}{r} \right)^{2+l} \theta_B,$$

Arons & Scharlemann 1979 *ApJ*.

$$\theta_x \approx \frac{B_\theta}{B_r} = -\frac{dP_l(\cos \theta)/d\theta}{(l+1)P_l(\cos \theta)} \approx \frac{l}{2} \theta$$

### III. ICS' impact on profiles' frequency dependence



B1642-03

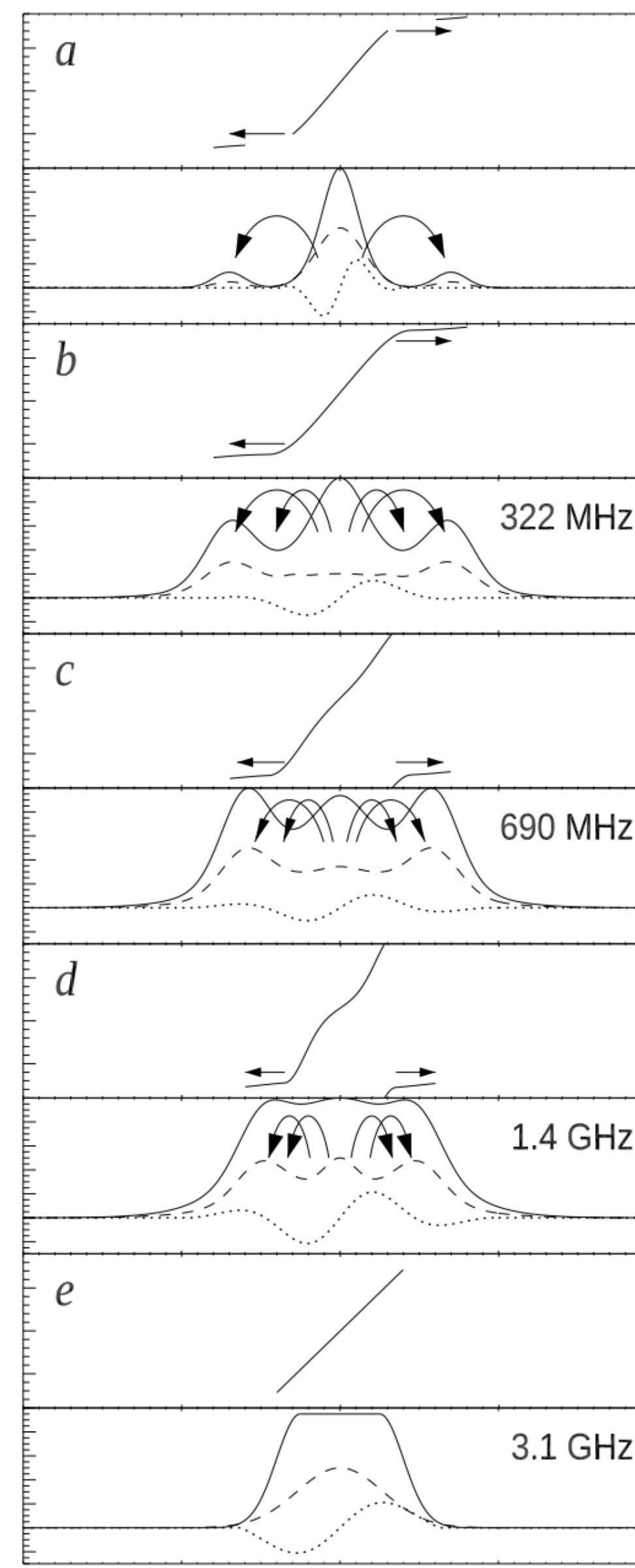
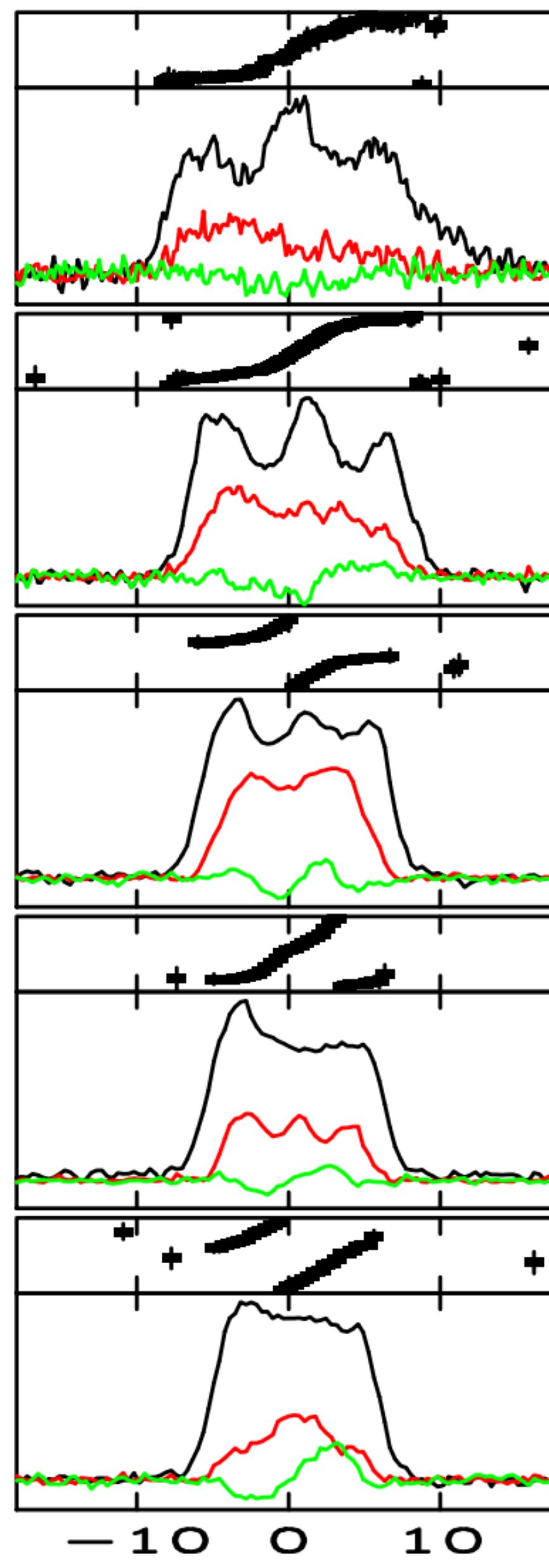
Conal components appear at high frequency:

They are scattered and blueshifted.

$$(\nu_1 = \gamma^2 \nu_0)$$

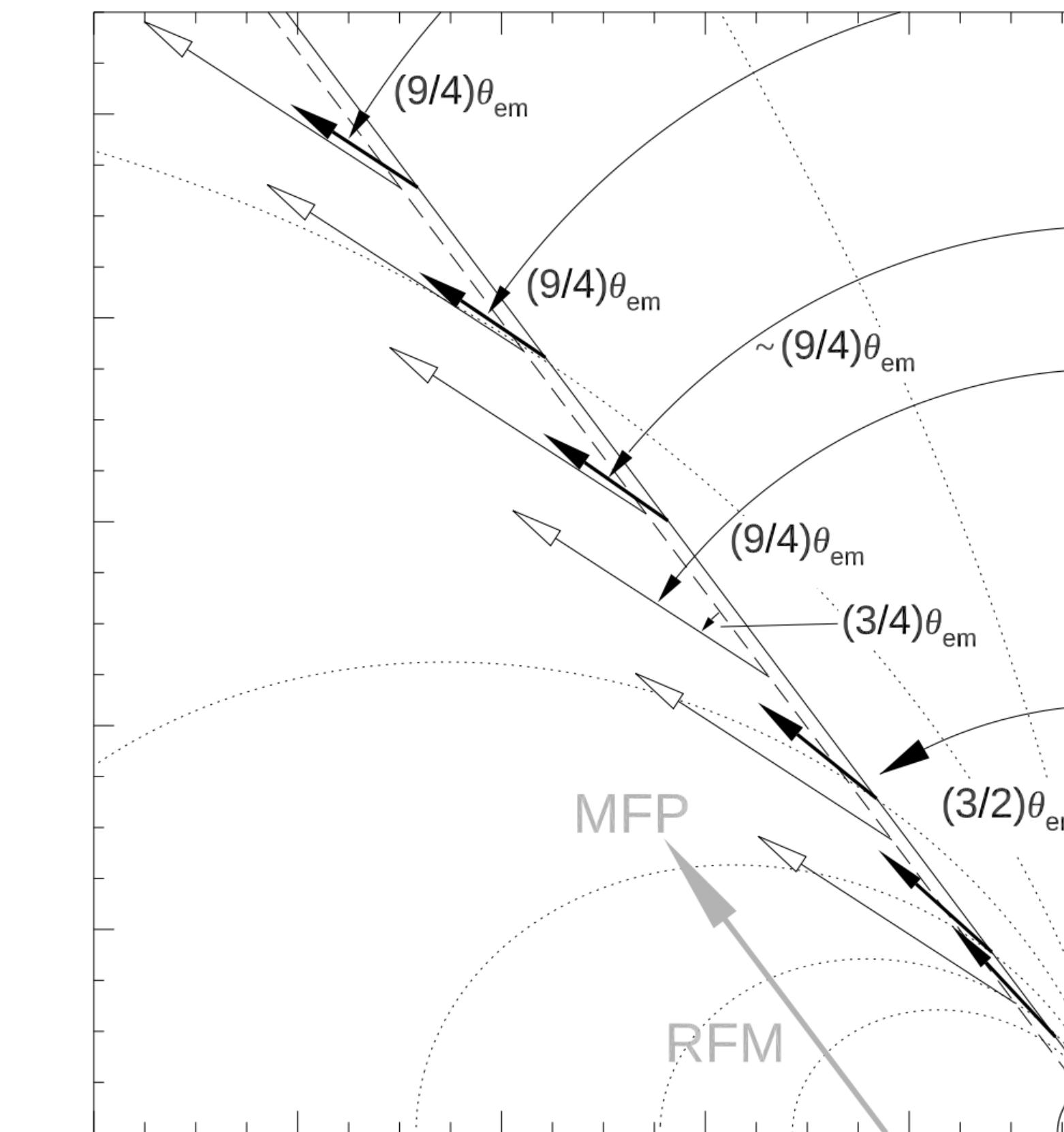
Different polarization modes are differently scattered

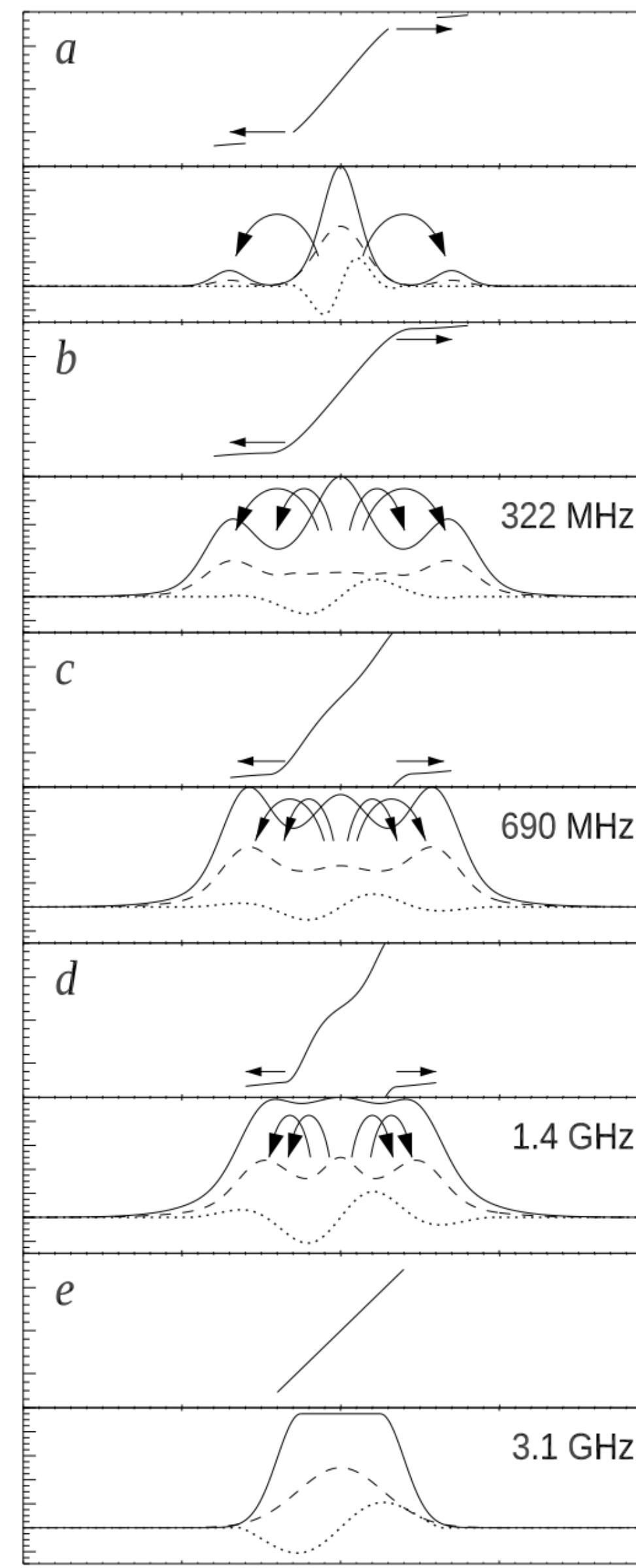
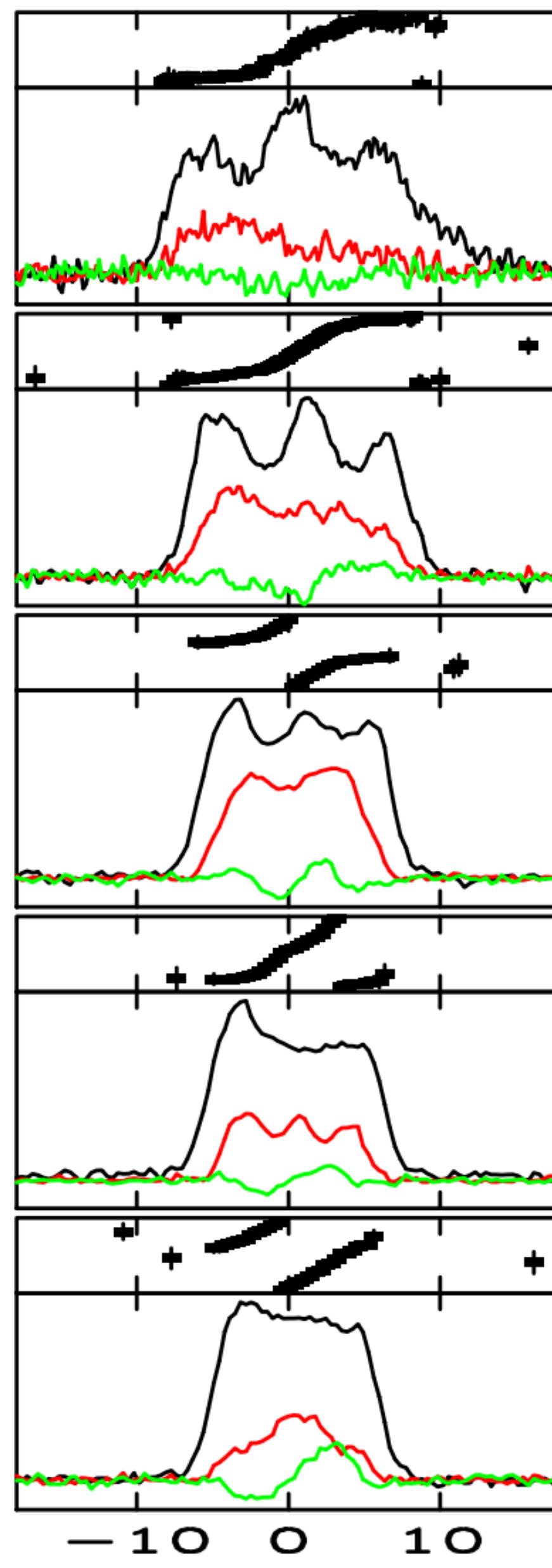
→ Different dominating modes for core/conal components



Mean free path should decrease with frequency:

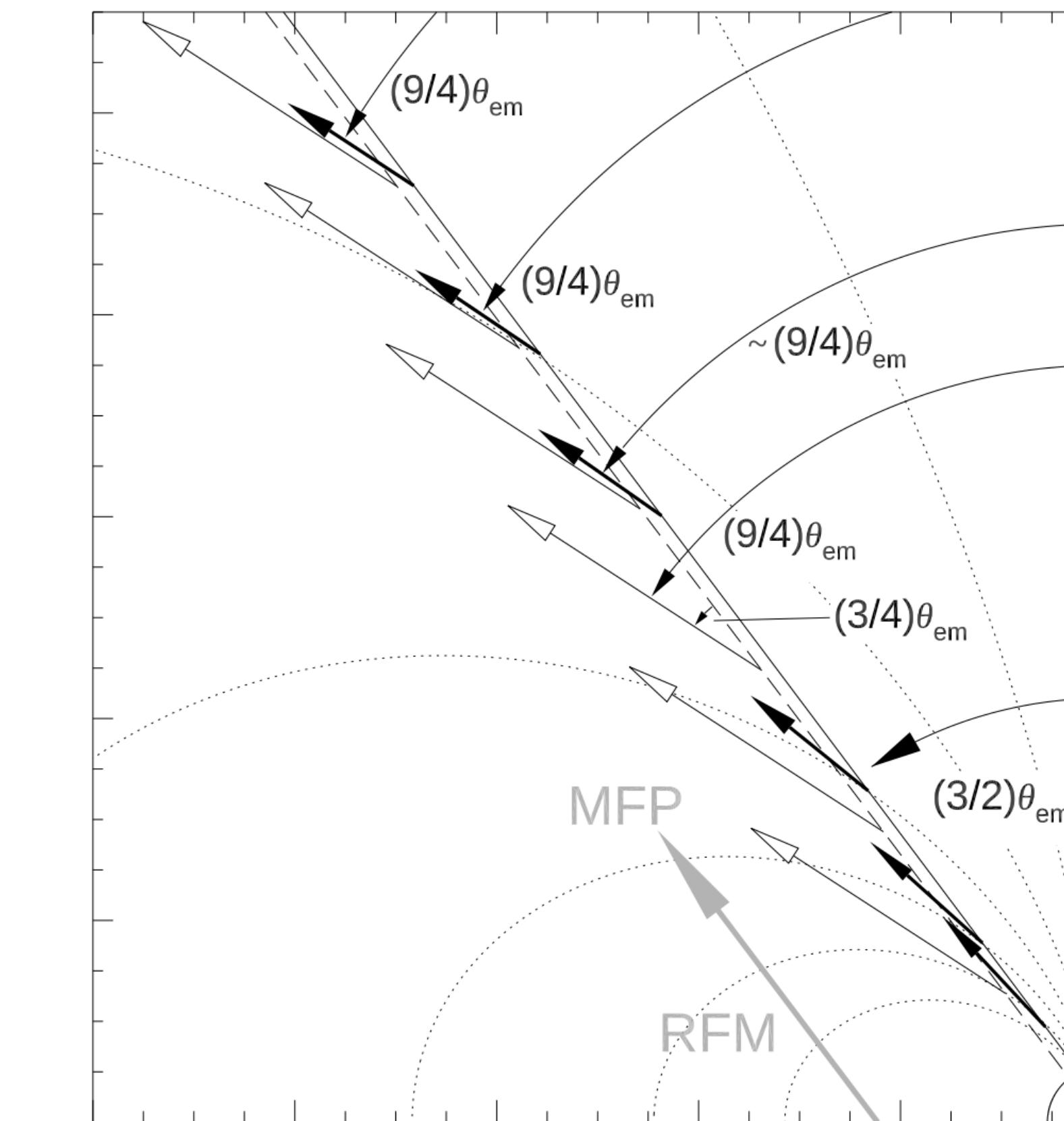
Higher frequency → lower scattering height  
 →→ Smaller scattering angle  
 →→ Narrower profile





Mean free path should decrease with frequency:

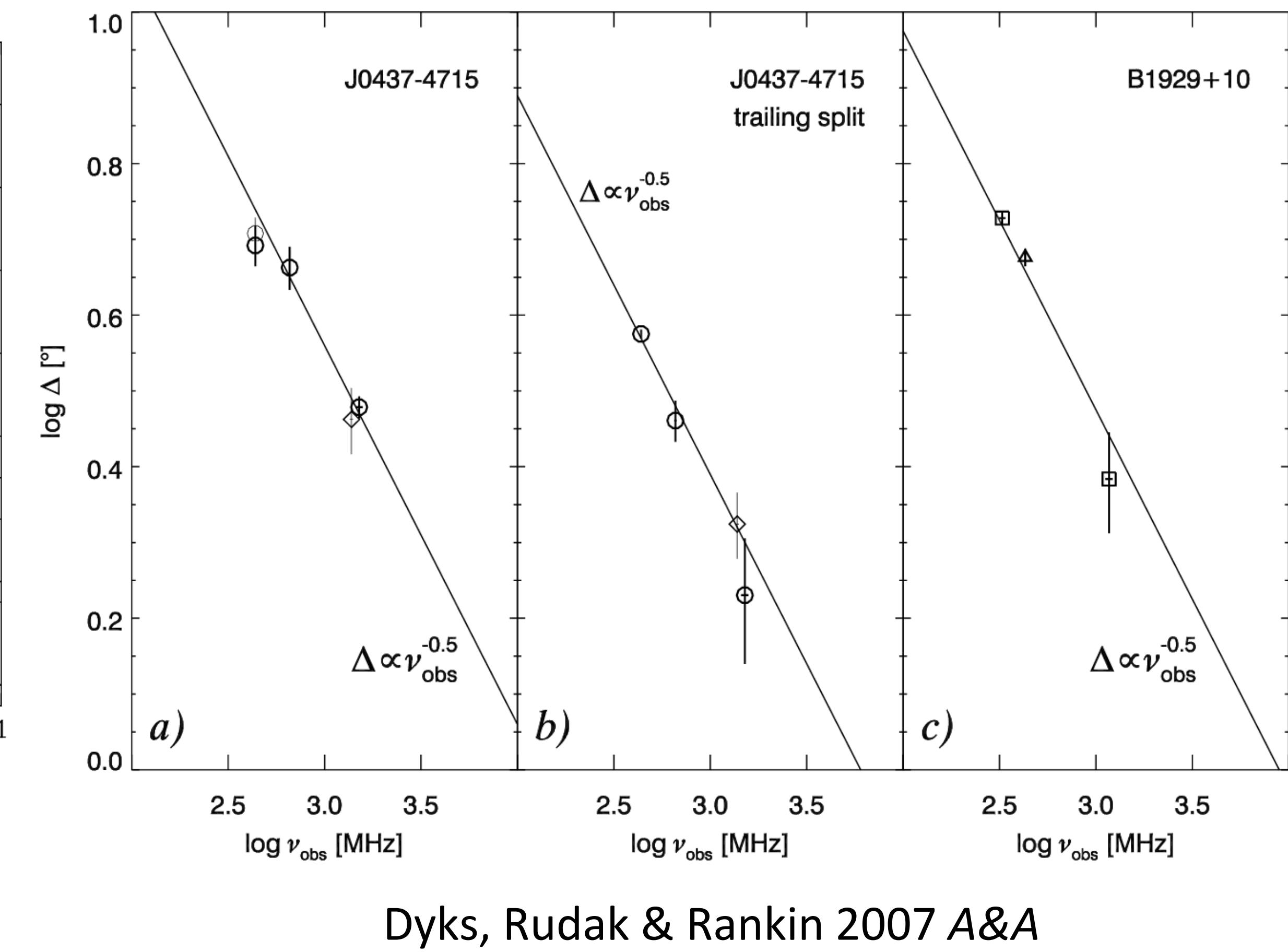
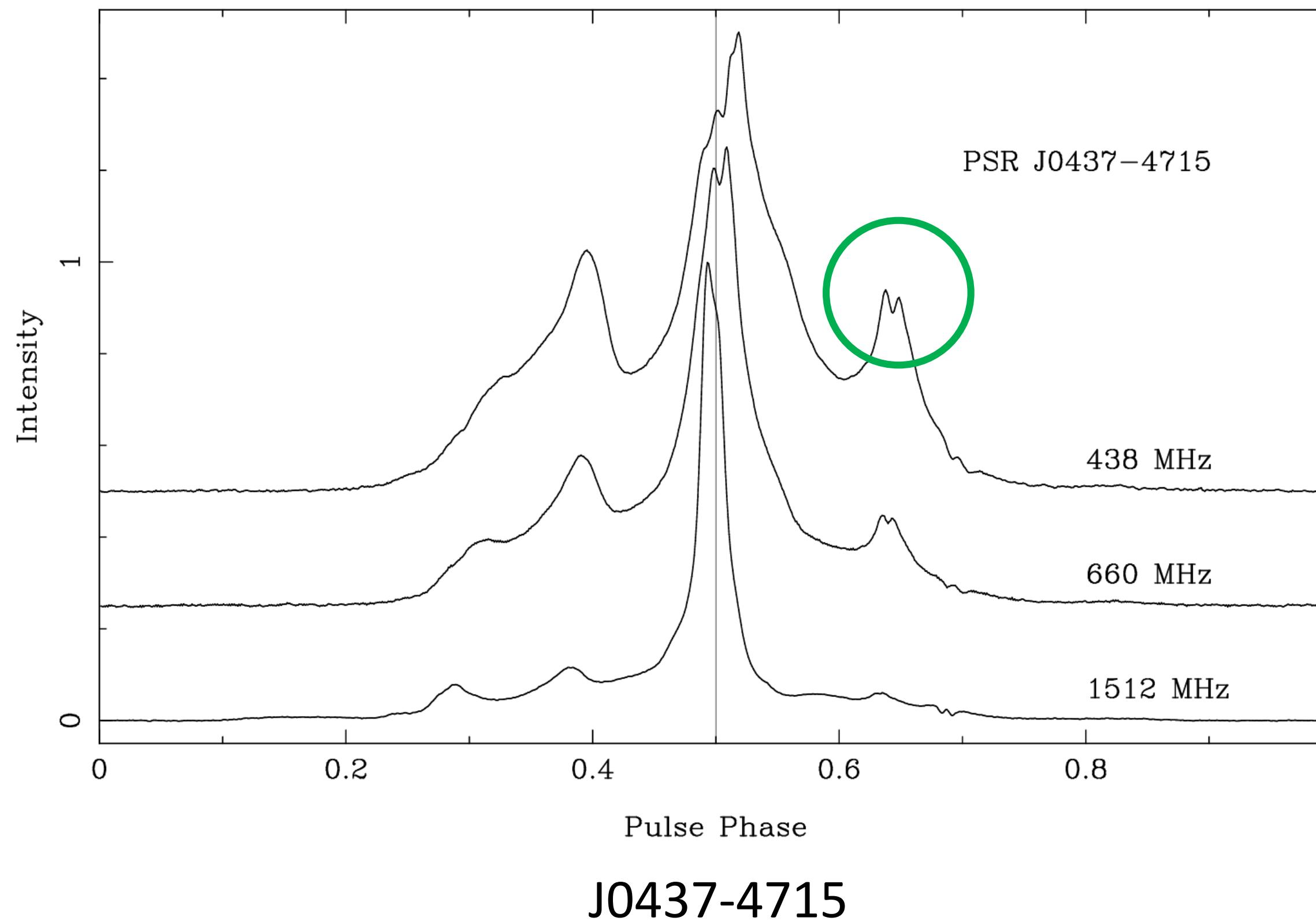
Higher frequency  $\rightarrow$  lower scattering height  
 $\rightarrow\rightarrow$  Different scattering angle  
 $\rightarrow\rightarrow$  Components' merging



# IV. Understand Bifurcated components

Two types of bifurcated components:

(1) Narrow conal components merging quickly with increasing frequency  $\Delta \propto \nu^{-1/2}$



Two types of bifurcated components:

(1) Narrow conal components merging quickly with increasing frequency  $\Delta \propto \nu^{-1/2}$

This kind of bifurcated components are scattered by electron flow of very small velocity direction spread.

$$\Delta \hat{v} \ll 1/\gamma_{sc}$$

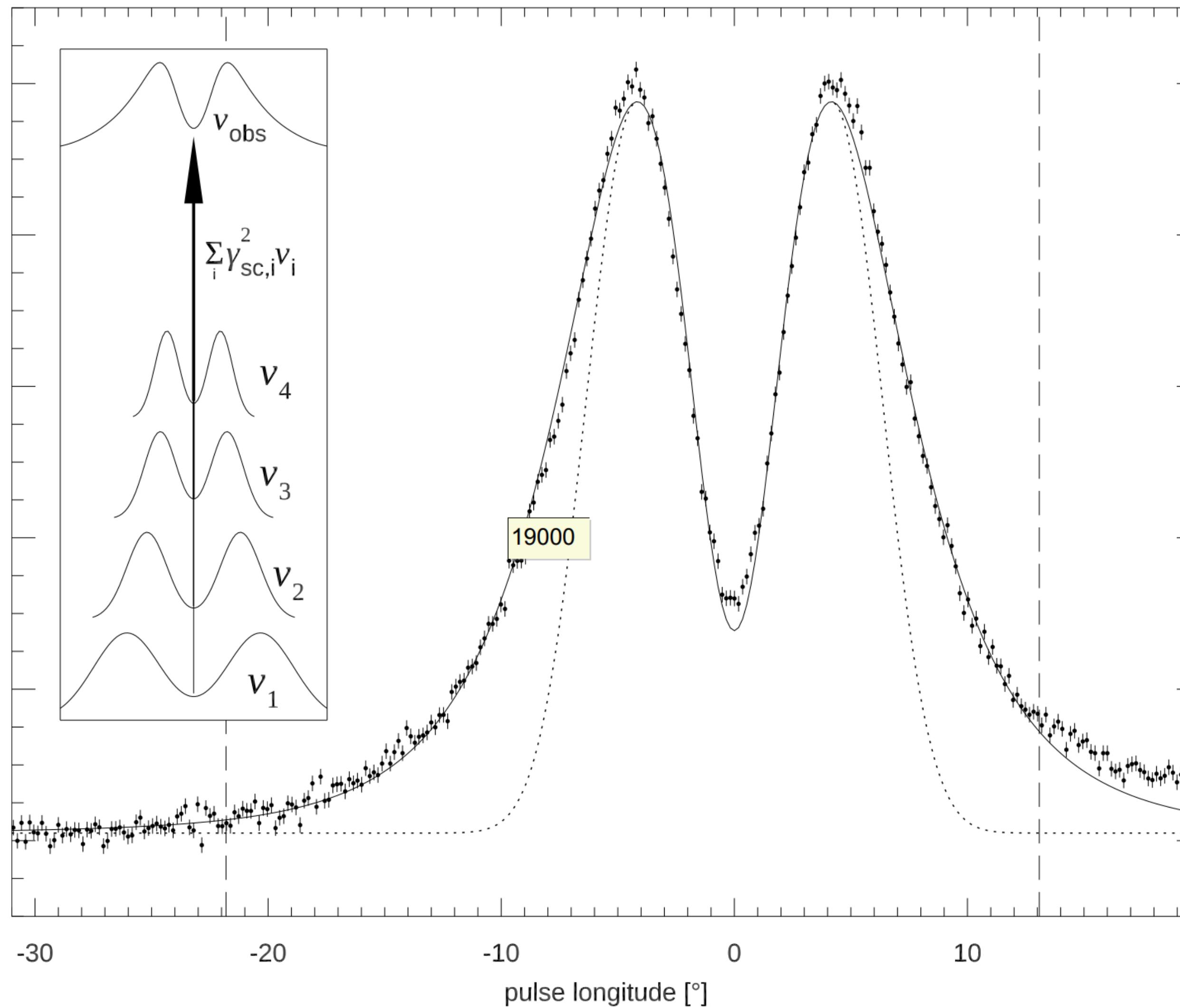
Beam width / components' separation:  $\Delta \propto 1/\gamma_{sc}$  (1/Lorentz factor of scattering particles).

For ICS:  $\nu_{obs} \approx \gamma_{sc}^2 \nu_{em}$

$$\rightarrow \Delta \propto (\nu_{em}/\nu_{obs})^{1/2}$$

Two types of bifurcated components:

(2) Wide, strong, and symmetric bifurcated components, merging with frequency slower.



$$\Delta \propto \nu^{-0.35}$$

The larger width results from scattering by particles with larger velocity spread.

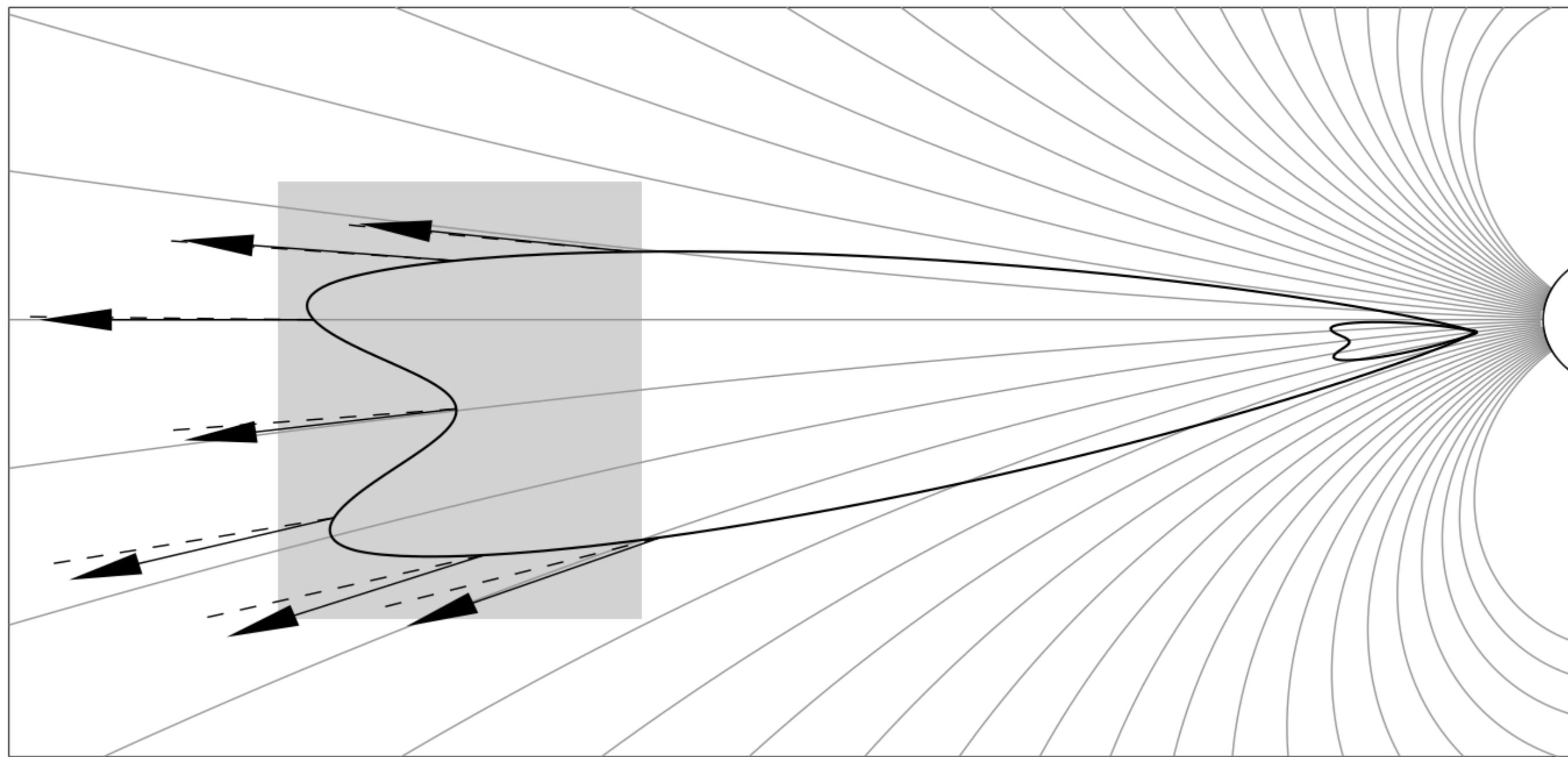
$$\Delta \hat{v} \gg 1/\gamma_{\text{sc}}$$

Dotted line: frequency-resolved curvature radiation beam (with only O-mode)

Solid line: frequency-integrated...  
(frequency-integrated performs better)

Two types of bifurcated components:

(2) Wide, strong, and symmetric bifurcated components, merging with frequency slower.

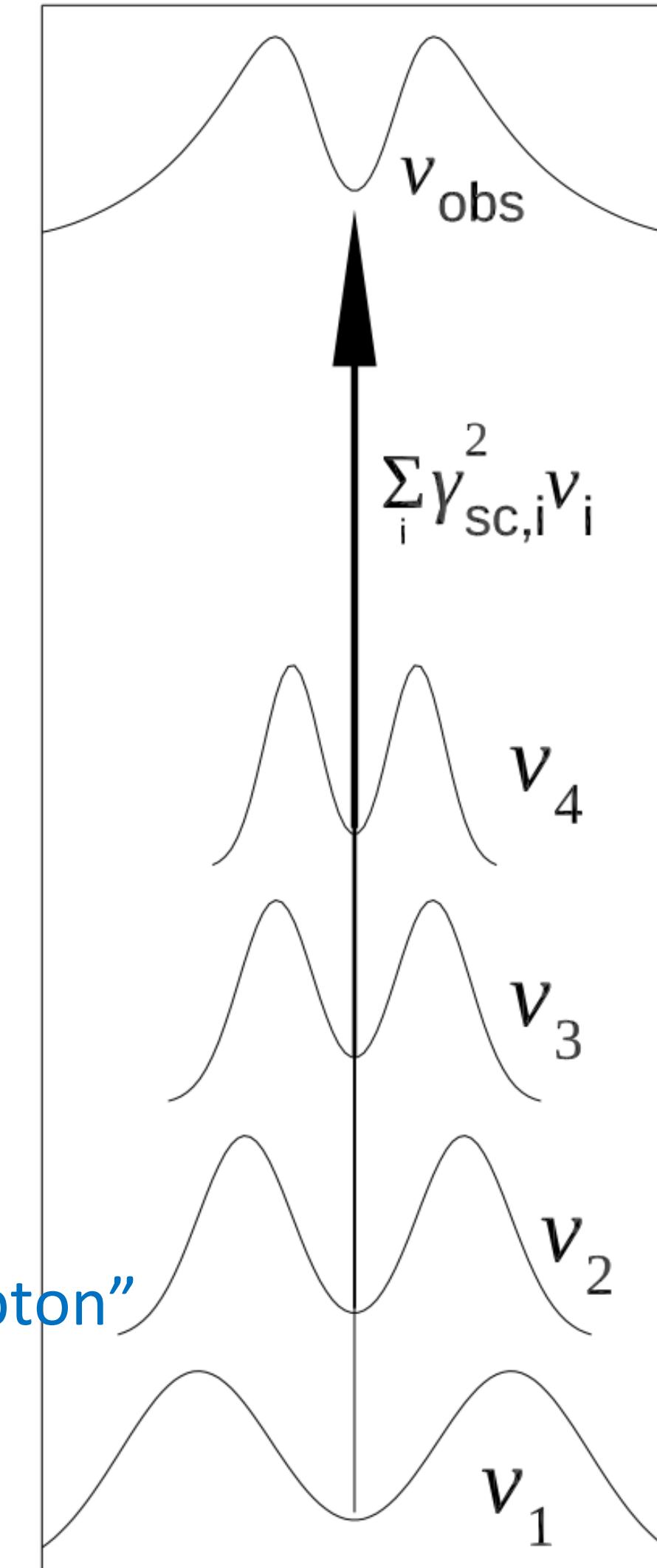


The larger width results from scattering by particles with larger velocity spread.

$$\Delta \hat{v} \gg 1/\gamma_{sc}$$

“Curvature self-Compton”

Profiles of different frequencies could be blueshifted  
To a same frequency ← origin of “frequency-integrated” CR beam.

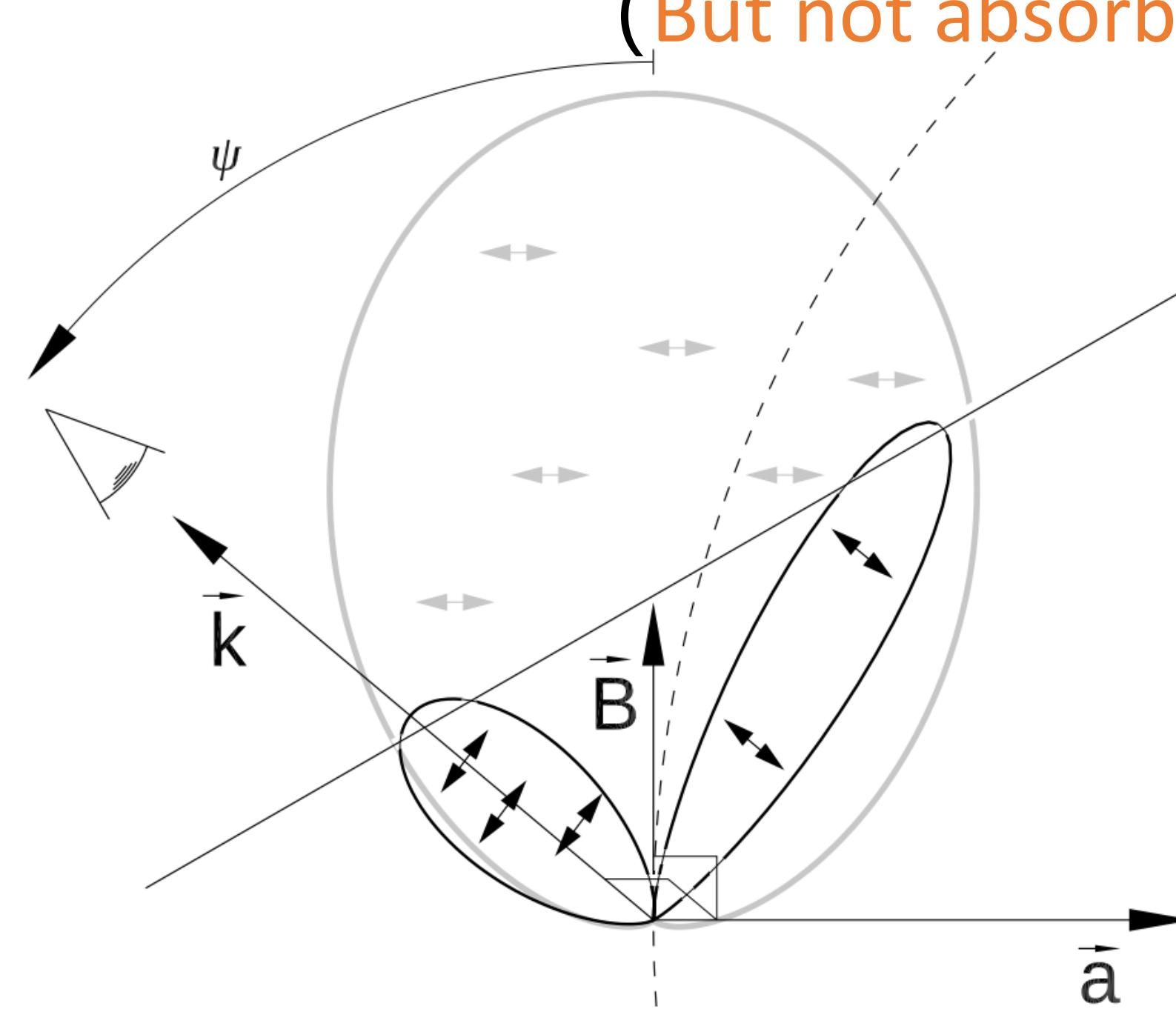


Two types of bifurcated components:

(2) Wide, strong, and symmetric bifurcated components, merging with frequency slower.

ICS of curvature radiated beam: components polarized within  $\mathbf{k} \times \mathbf{B}$  plane could be effectively scattered.

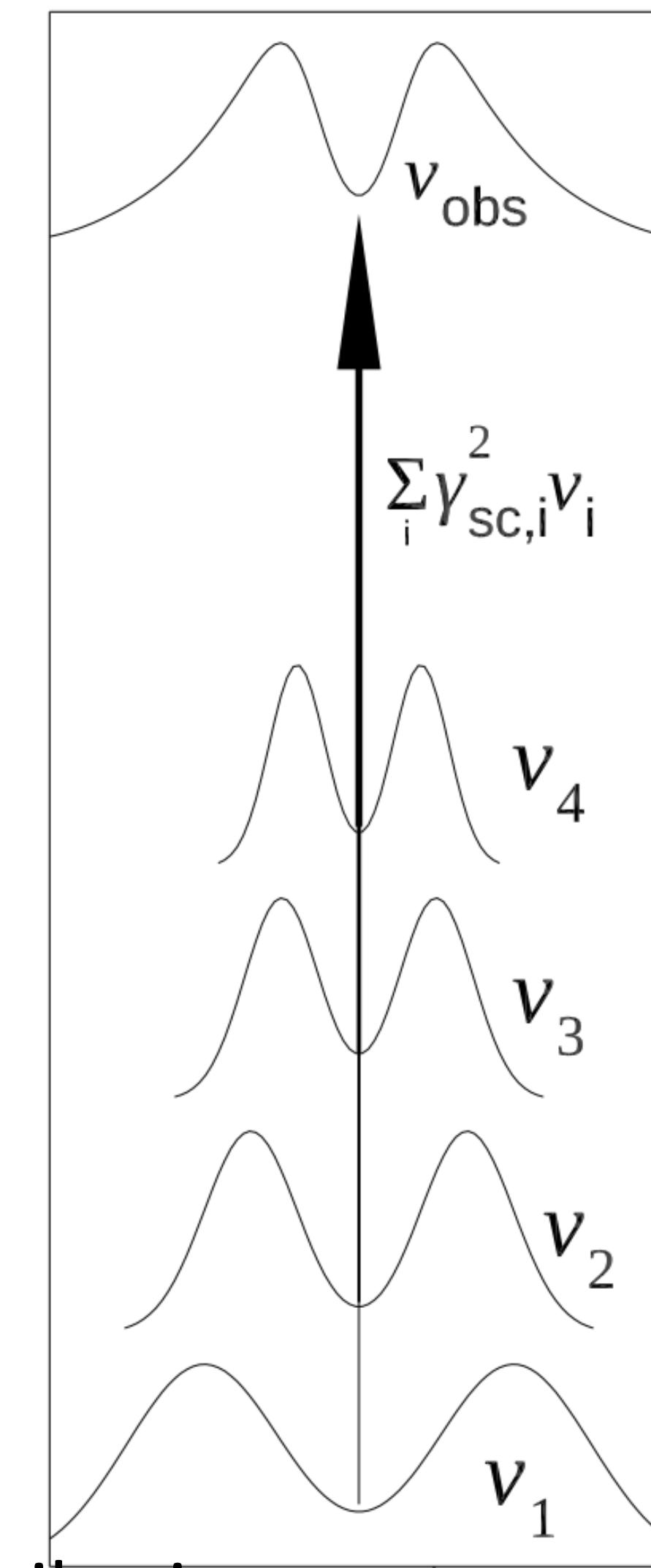
(But not absorbed yet...?)



Emitting particle with  $\gamma \sim 10$ : CR freq  $\sim 1$  MHz.

Observed frequency  $\sim 1$  GHz  $\rightarrow \gamma_{sc} \sim 30$ .

Scattering particles and emitting particles could have same energy distribution.



# V. Discussion

## (1) Implications for subpulse modulation:

Scattering modifies beam structure & spectral properties.

→ Temporal variations of electron energy spectrum could lead to flux modulation.

## (2) Cones or fan beams?

The answer is ambivalent at present...

The geometry behind conal structure may not be conal because of scattering.

**Summary: ICS of curvature radiation in pulsar magnetic field  
could explain conal structures and bifurcated components.**

**Thank you for your attention ☺**